



Impedance Matching for Wave Driven Desalination Systems

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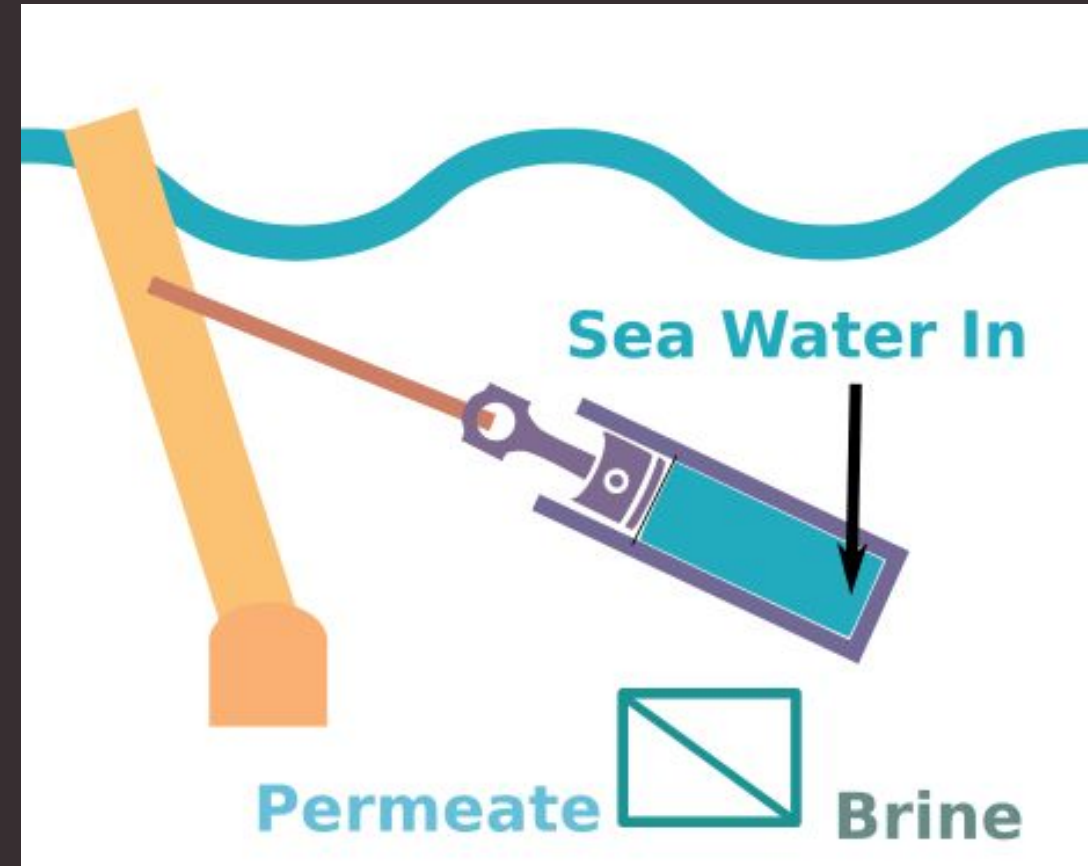
Presented by Nate DeGoede

Agenda

- Background
 - **Wave Driven Desalination**
 - Impedance Matching
- Overview of Dynamics
- **DesalOptTool**
 - Current Issues
 - Future Steps
- Anticipated Impacts

Wave Driven Desalination

- Clean water access is a growing concern [1]
- Direct Drive Desalination [2,3]
 - Wave Energy Converters (WECs) **harness mechanical energy**
 - Desalination **needs mechanical energy**
- Potential niche market where WECs can develop [4]



Impedance Matching

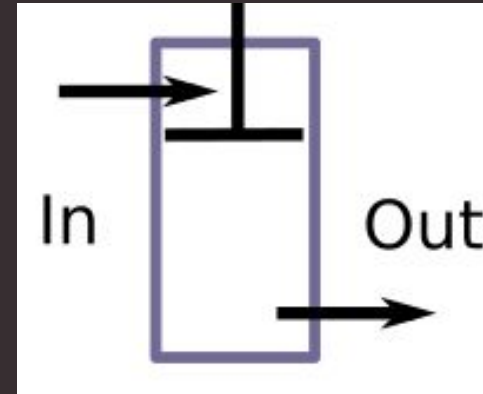
- **Impedance** = “Effort”/“Flow”
- Impedance of WEC & Power Take Off (PTO) “matches” the excitation [5]
- 22% improvement in WEC performance for electricity generating PTOs [6]
- Can we apply to wave driven desalination?



Dynamics (Piston)

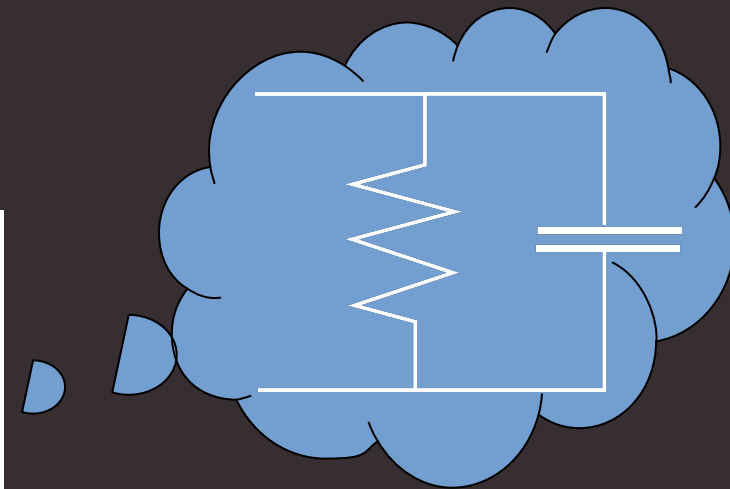
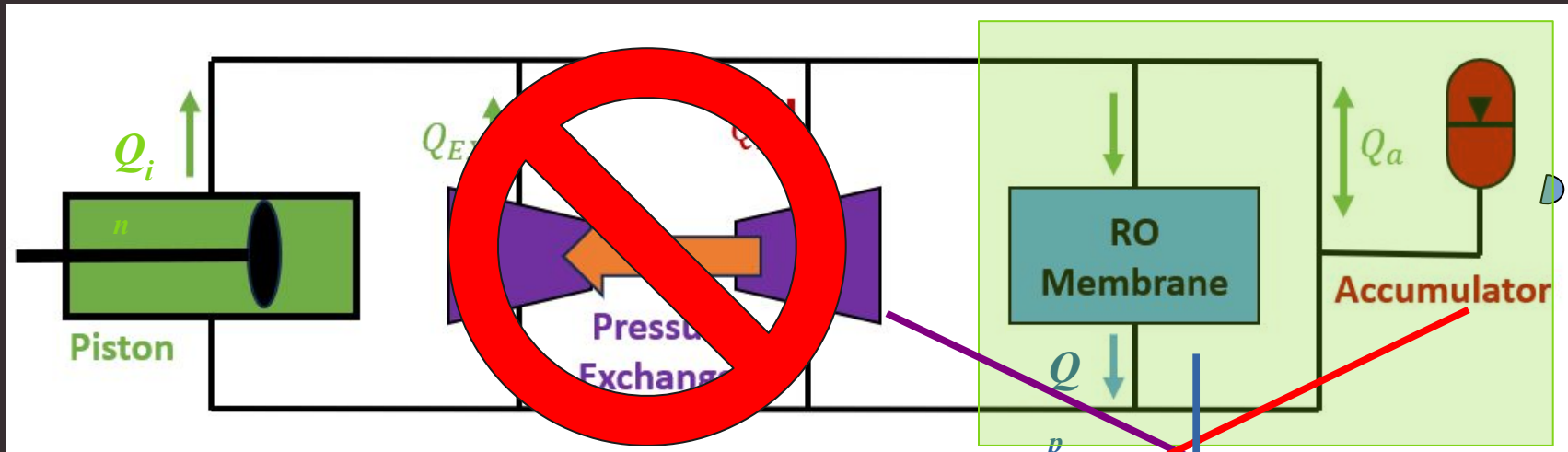
$$A|v| = Q_{in}$$
$$|F_{PTO}| = AP$$

Force always opposes velocity



A	Piston area
v	Piston velocity
Q_{in}	Seawater flow rate into hydraulic circuit
F_{PTO}	Force on WEC due to PTO
P	Pressure of fluid in hydraulic circuit

Dynamics (Hydraulic Circuit)



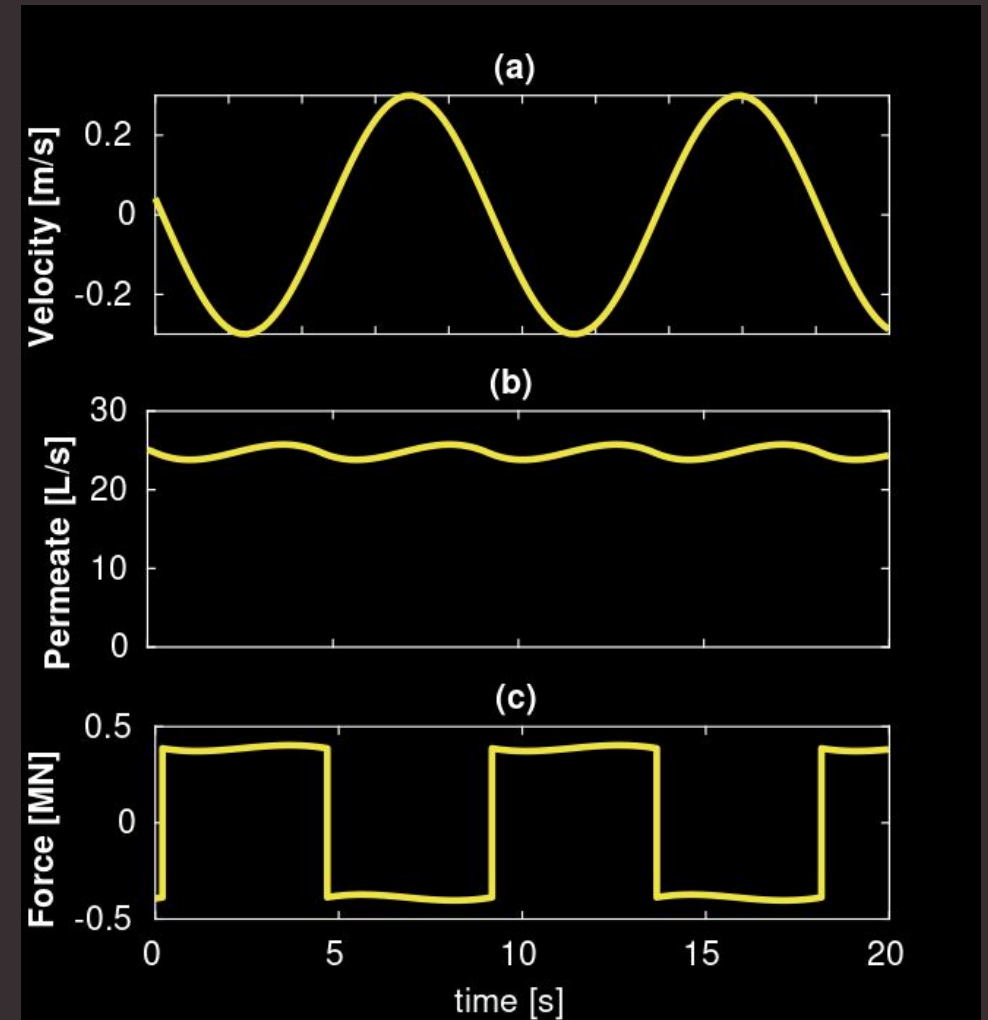
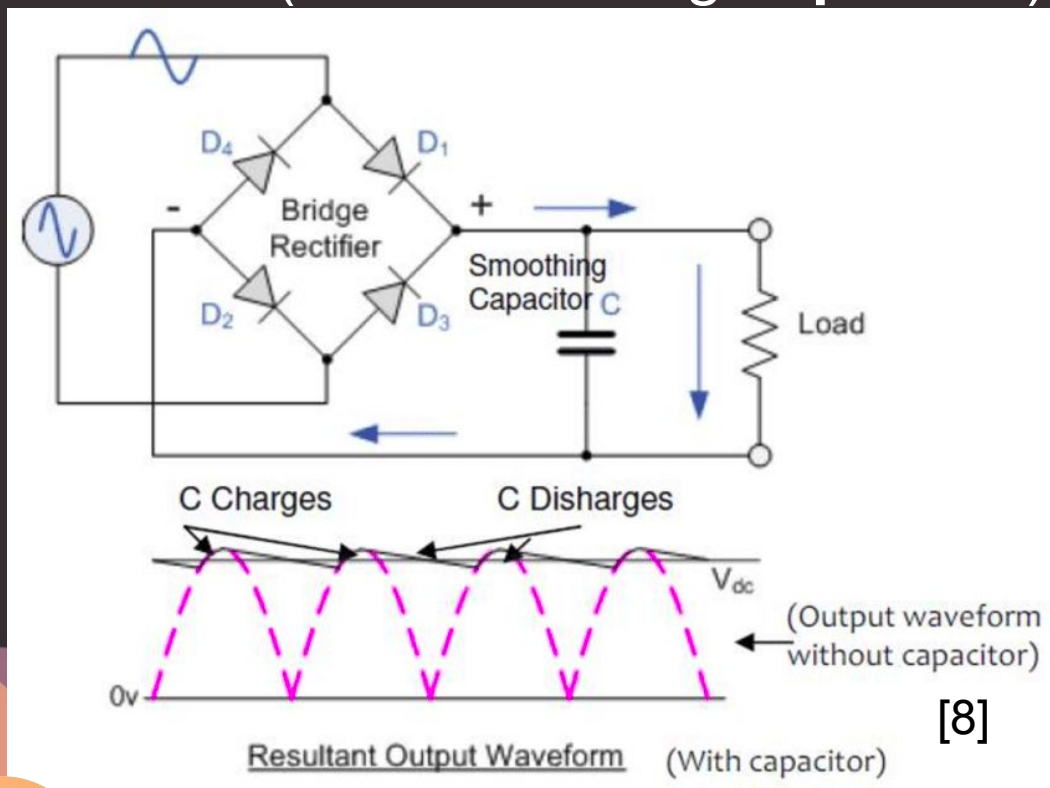
$$0 = Q_{in} - C_a \frac{dP(t)}{dt} - \frac{P(t)}{R_m} - \frac{P(t)}{R_t}$$

$$Z_h(j\omega) = \frac{P(j\omega)}{Q_{in}(j\omega)} = \frac{1}{j\omega C_a + \frac{1}{R_m} + \frac{1}{R_t}}$$

Q_{in}	Seawater flow rate from Piston
C_a	Accumulator Capacitance
P	Pressure of fluid in hydraulic circuit
$R_{m/t}$	Resistance of Membrane/Brine valve
Z_h	Hydraulic Impedance

Dynamics (Combined)

Dynamics are similar to a **full wave bridge rectifier** (with smoothing capacitor)



Notice the force signal **discontinuities**

DesalOptTool (Overview)

- Add-on package for **WecOptTool**
 - Pseudospectral domain [9]
 - Control co-design (CCD) [6]
- Expand ideas in wave driven desalination
 - CCD
 - Impedance matching
 - Wave to water Multidisciplinary Design Optimization (MDO)

DesalOptTool (Current Issue)

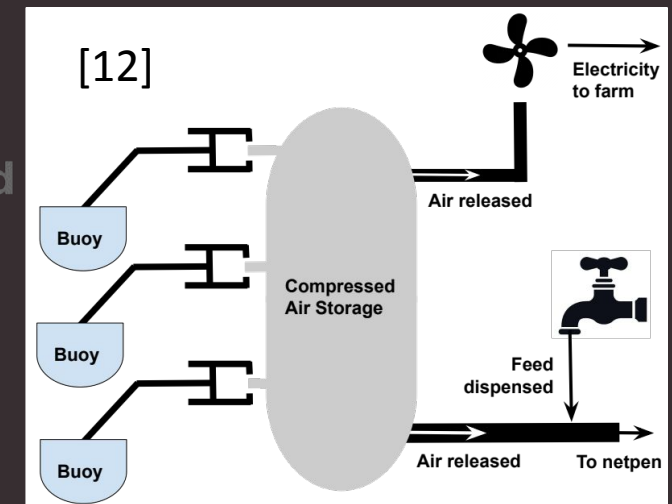
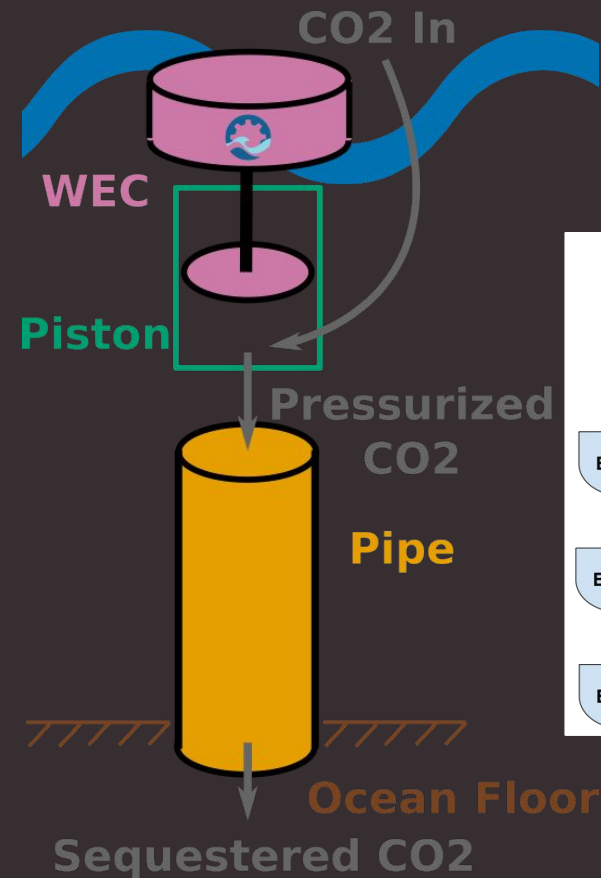
- Challenging dynamics
- Force is **discontinuous**
- **Check valves** cause PTO force to sometimes behave like static friction
 - **When excitation force is below PTO force \rightarrow velocity = 0**

DesalOptTool (Future Work)

- Fix dynamics issue
 - Will likely require adjustment of core module
- Add in multiple DOF functionality
- Model other hydraulic components
 - Bladder style accumulator
 - Pressure exchanger
 - Fluid inertia
- Improve packaging

DesalOptTool (Anticipated Impacts)

- Tool for **MDO** in Wave Driven Desalination
 - CCD
 - **Wave to water** analysis
- Dynamics for other PTOs
 - Hydraulic drivetrains [10]
 - **Carbon sequestration** [11]
 - **Aquaculture feeding system** [12]



Summary

- **Dynamics** involved in Wave Driven Desalination
 - Piston
 - Accumulator
 - **Discontinuous** Force
- **DesalOptTool**
 - Potential tool for **Wave to water MDO**
 - Dynamics pose problem
- Extensions of this work to **other applications**

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Questions?

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