



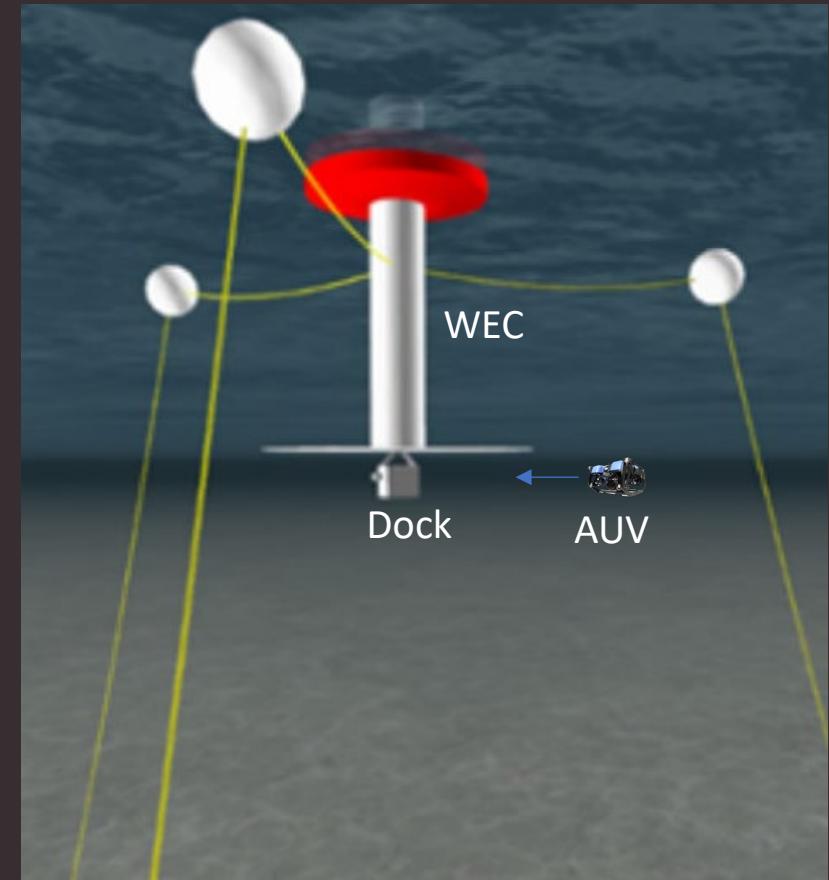
Hardware-in-the-Loop Testing for Autonomous Underwater Vehicle Docking in Dynamic Ocean Waves

Junhui Lou, David Okushemiya, Bryson Robertson

Oregon State University

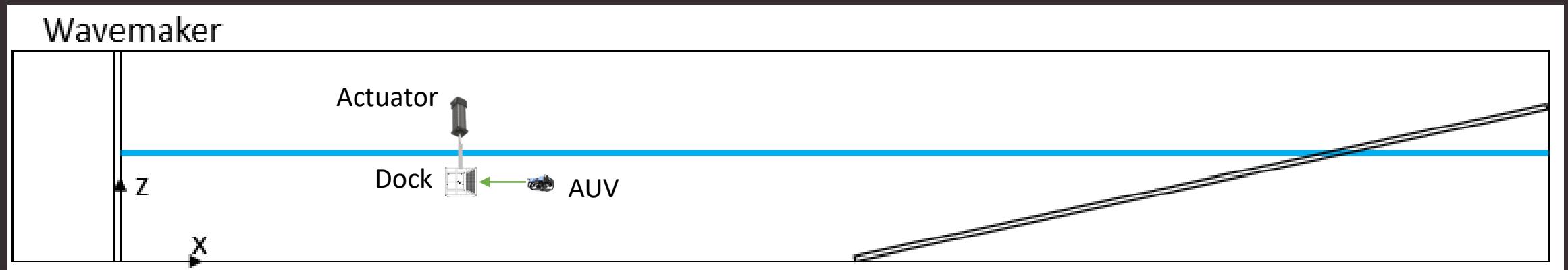
AUV powered by WEC

- Autonomous underwater vehicles (AUVs)
 - Wide range of maritime applications in ocean exploration
 - Range and duration are limited by battery capacity
- Wave energy converters (WECs)
 - Harvest ocean wave energy that is consistent and predictable
 - Charge AUV onsite enhancing AUV mission capacity
- Integrate AUV with WEC
 - Docking station attached to the WEC directly
 - Increased docking difficulty as AUV navigates and docks near the ocean surface, encountering significant wave force



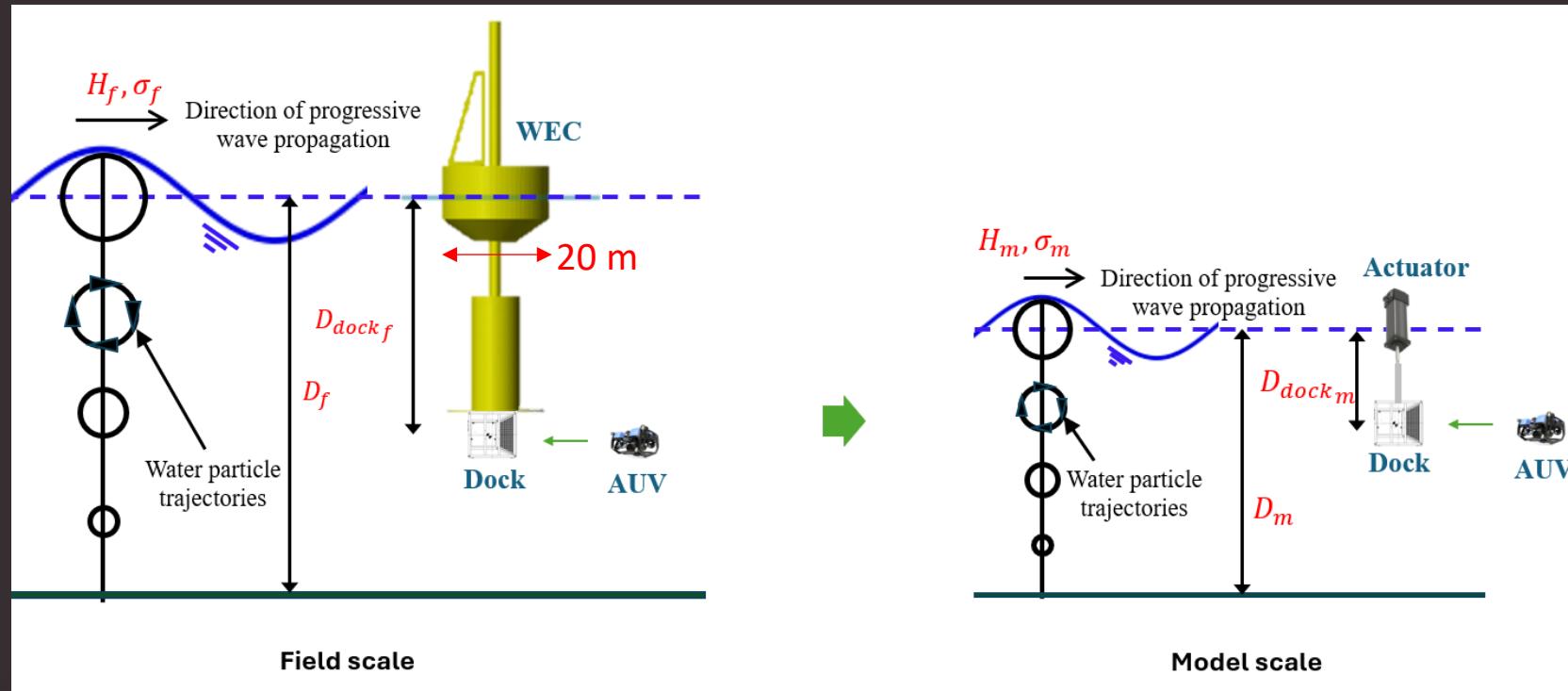
Research Question

- This study investigated the experimental testing procedure of AUV docking on a WEC in the wave flume.
- How to test AUV docking through a mixed-scale approach with waves and dock motions synchronized in real time?



Mixed-scale Approach

- Testing AUV docking in the wave flume requires a mixed-scale approach
 - Full-scale AUV and dock, model-scale waves
 - Goal: replicate the wave-induced force on AUV and the dynamic motion of the dock in the laboratory



Wave Force on AUV

- Wave-induced forces on AUV calculated by Morison equation:

$$F = \underbrace{\rho C_m V \dot{u}_r}_{F_I} + \underbrace{1/2 \cdot \rho C_d A u_r |u_r|}_{F_D}$$

F_I is the inertia force, depends on water particle acceleration \dot{u}_r

F_D is the drag force, depends on water particle velocity u_r

Wave and Dock Motion Distortion (Inertia force dominant)

- **Inertia force dominant** scenario
 - Model-scale water acceleration = Field-scale water acceleration

$$a_{\text{water}_f}(\sigma_f) = a_{\text{water}_m}(\sigma_m)$$

- Model-scale dock acceleration = Field-scale dock acceleration

$$a_{\text{dock}_f}(\sigma_f) = a_{\text{dock}_m}(\sigma_m)$$

- The following conditions are required for matching acceleration

$$\frac{D_{\text{dock}_m}}{D_{\text{dock}_f}} = \frac{D_m}{D_f} = \lambda \quad (\text{Froude scale factor})$$

$$\frac{\sigma_m}{\sigma_f} = \lambda^{-0.5}$$

$$\frac{H_m}{H_f} = \lambda$$

$$\frac{A_{\text{dock}_m}}{A_{\text{dock}_f}} = \lambda$$

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Follow Froude
scale law

Wave and Dock Motion Distortion (Drag force dominant)

- **Drag force dominant** scenario
 - Model-scale water velocity = Field-scale water velocity

$$v_{\text{water}_f}(\sigma_f) = v_{\text{water}_m}(\sigma_m)$$

- Model-scale dock velocity = Field-scale dock velocity

$$v_{\text{dock}_f}(\sigma_f) = v_{\text{dock}_m}(\sigma_m)$$

- The following conditions are required for matching velocity

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$$\frac{H_m}{H_f} = \lambda^{0.5}$$

$$\frac{A_{\text{dock}_m}}{A_{\text{dock}_f}} = \lambda^{0.5}$$

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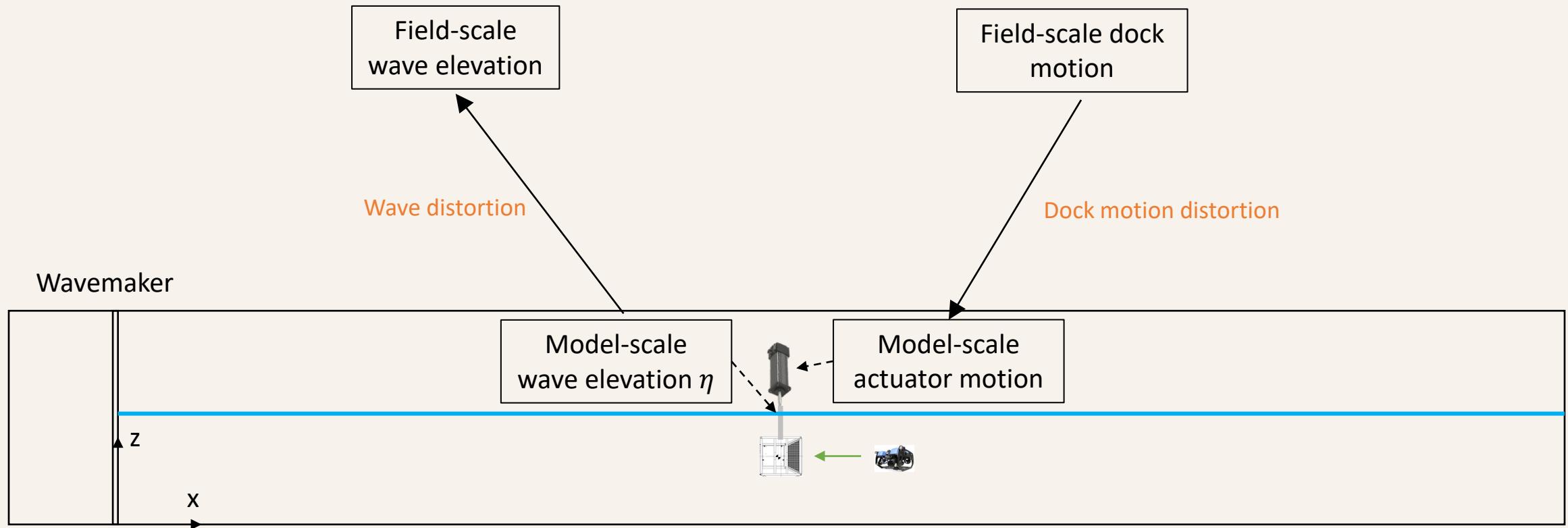
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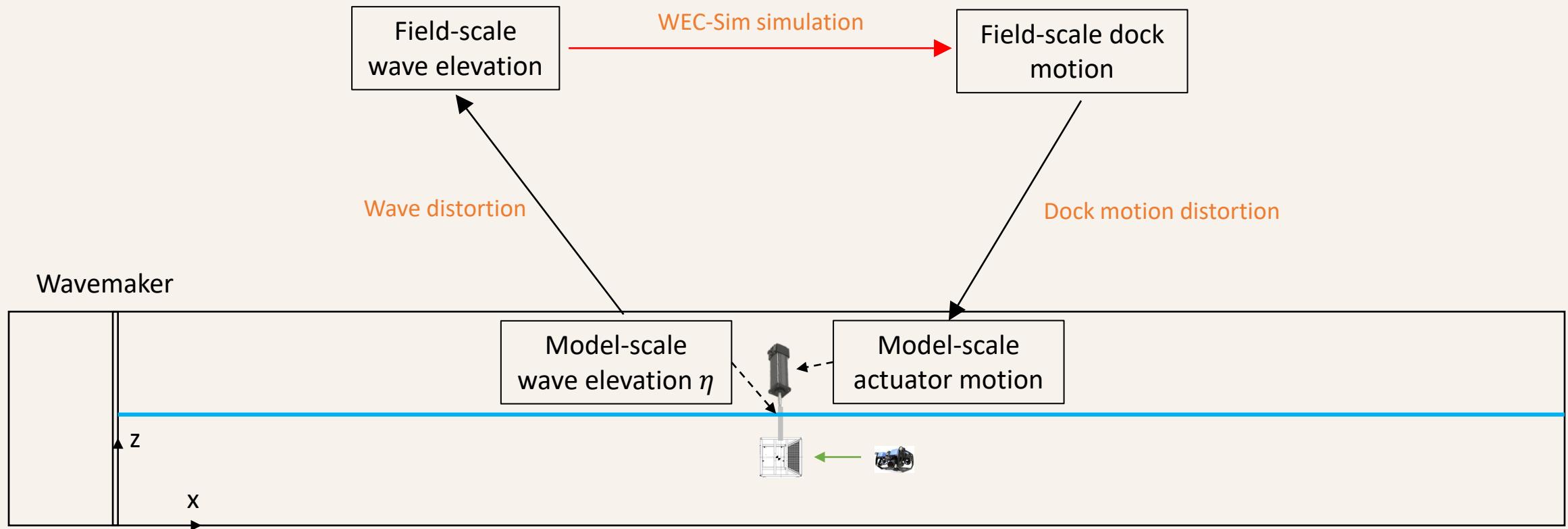
$$\frac{A_{\text{dock}_m}}{A_{\text{dock}_f}} = \lambda^{0.5}$$

Not follow Froude
scale law

Mixed-scale real-time testing procedure

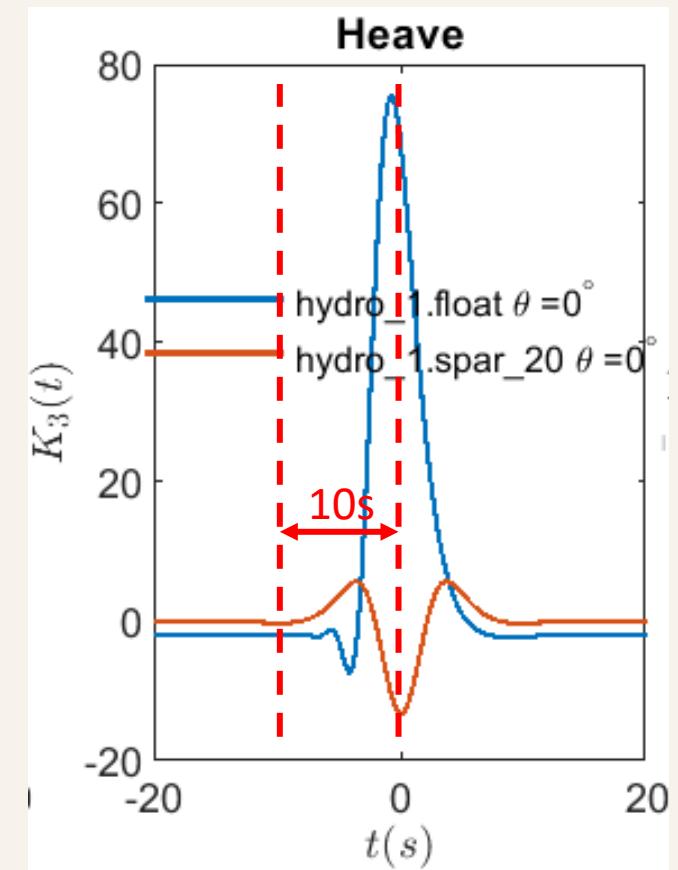


Mixed-scale real-time testing procedure

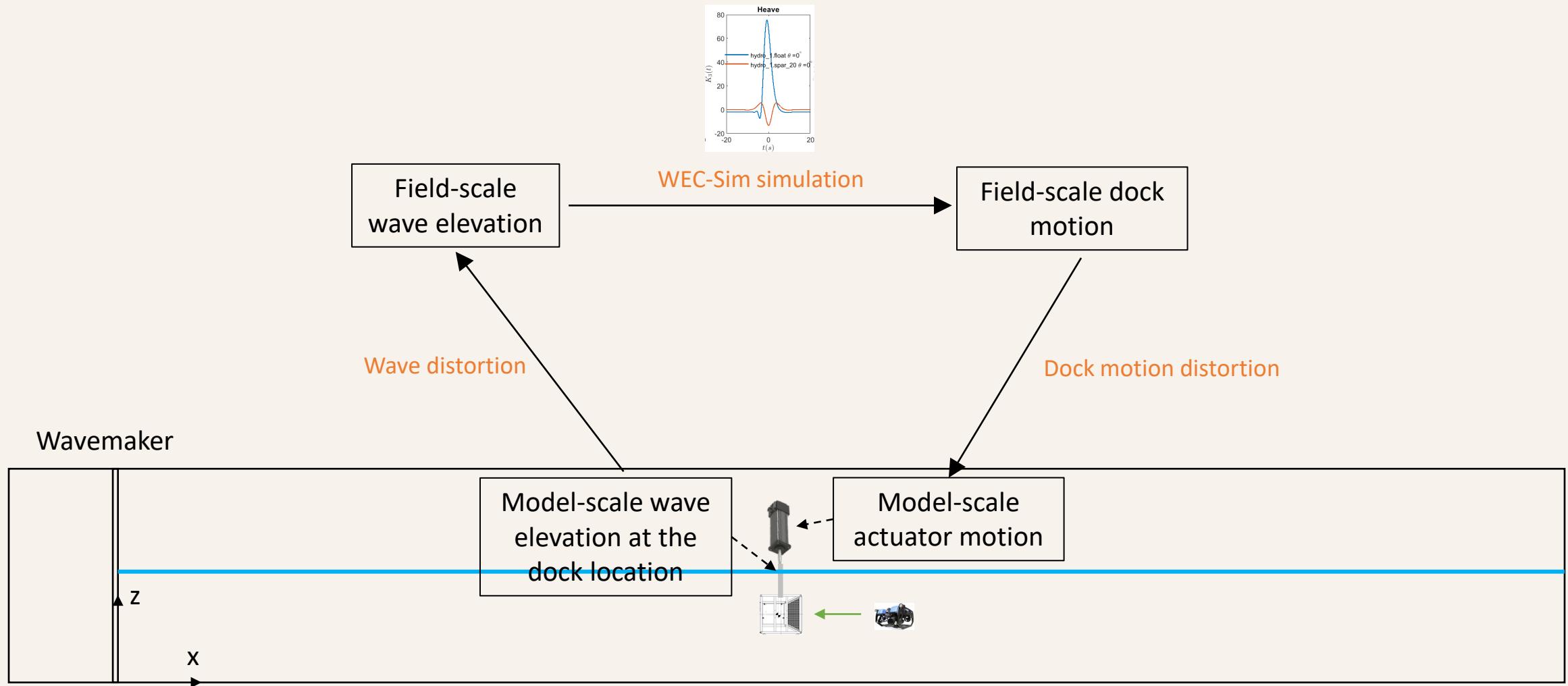


Non-causal Impulse Response $h(t)$

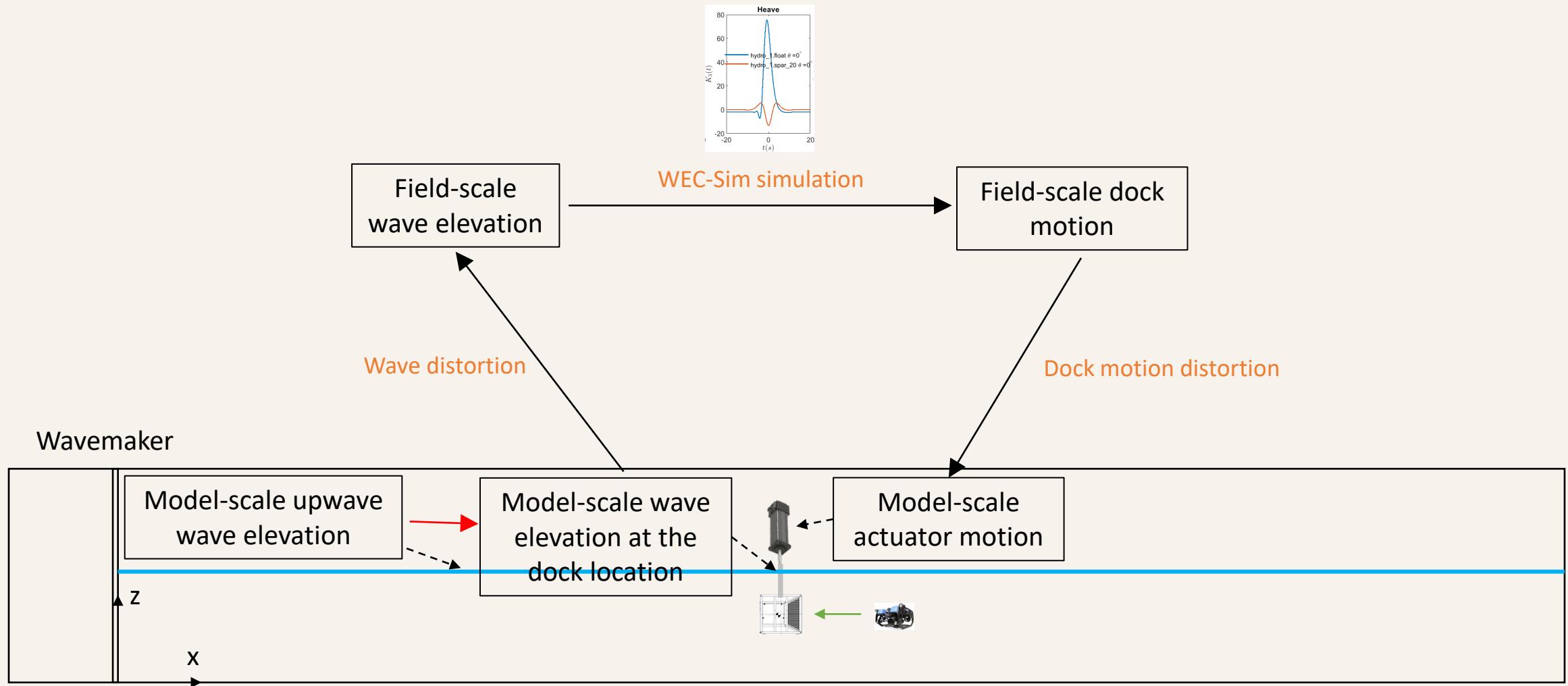
- Transfer function
 - $H(f) = \text{fft}(F(t))/\text{fft}(\eta(t))$
- Excitation impulse response function →
 - $h(t) = \text{ifft}(H(f))$
 - 10 s of leading wave elevation for LUPA 20 m
- $F(t) = \text{conv}(\eta(t), h(t))$



Mixed-scale real-time testing procedure

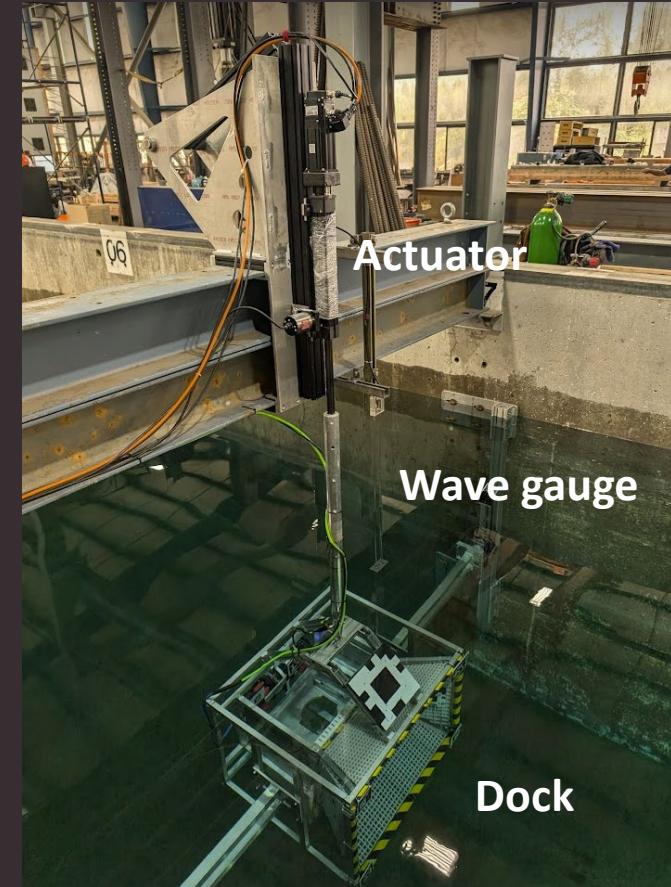


Mixed-scale real-time testing procedure



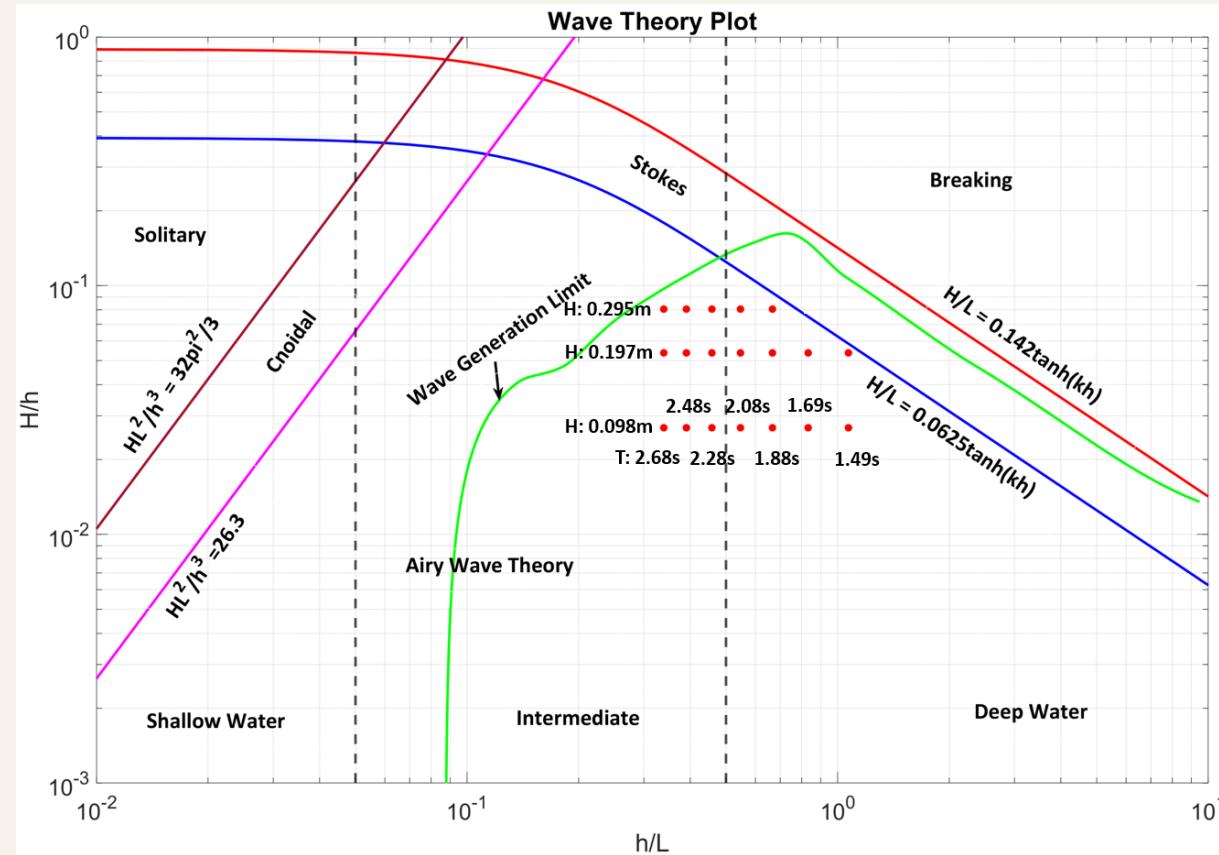
Laboratory Testing Considerations

- Large wave flume at O.H. Hinsdale Wave Research Laboratory
 - Water depth, wavemaker capacity
- Actuator
 - Stroke, velocity
- Wave gauge location



2024 WEC-AUV docking test

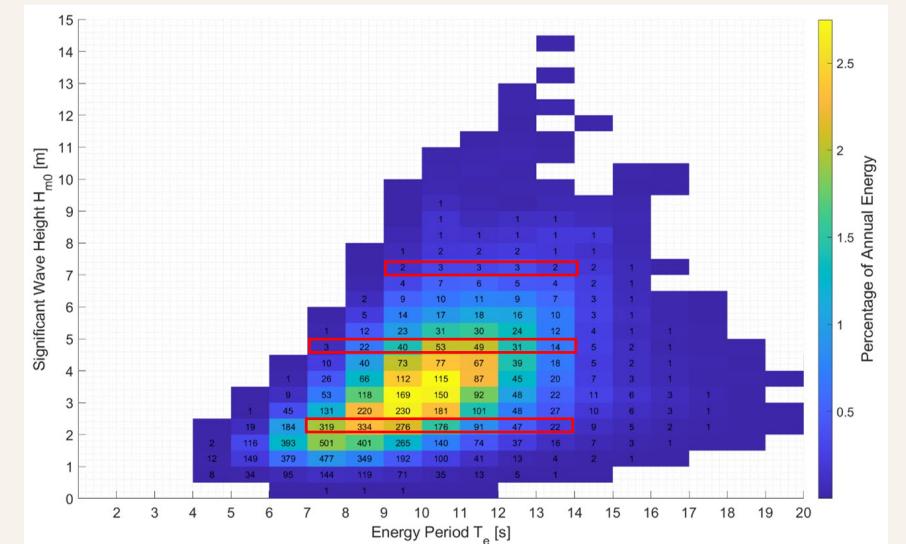
Model-Scale and Field-Scale Wave Conditions (acceleration matching)



Selection Of Model-scale Wave Conditions Within the Wave Generation Limit
and Wave Breaking Limit

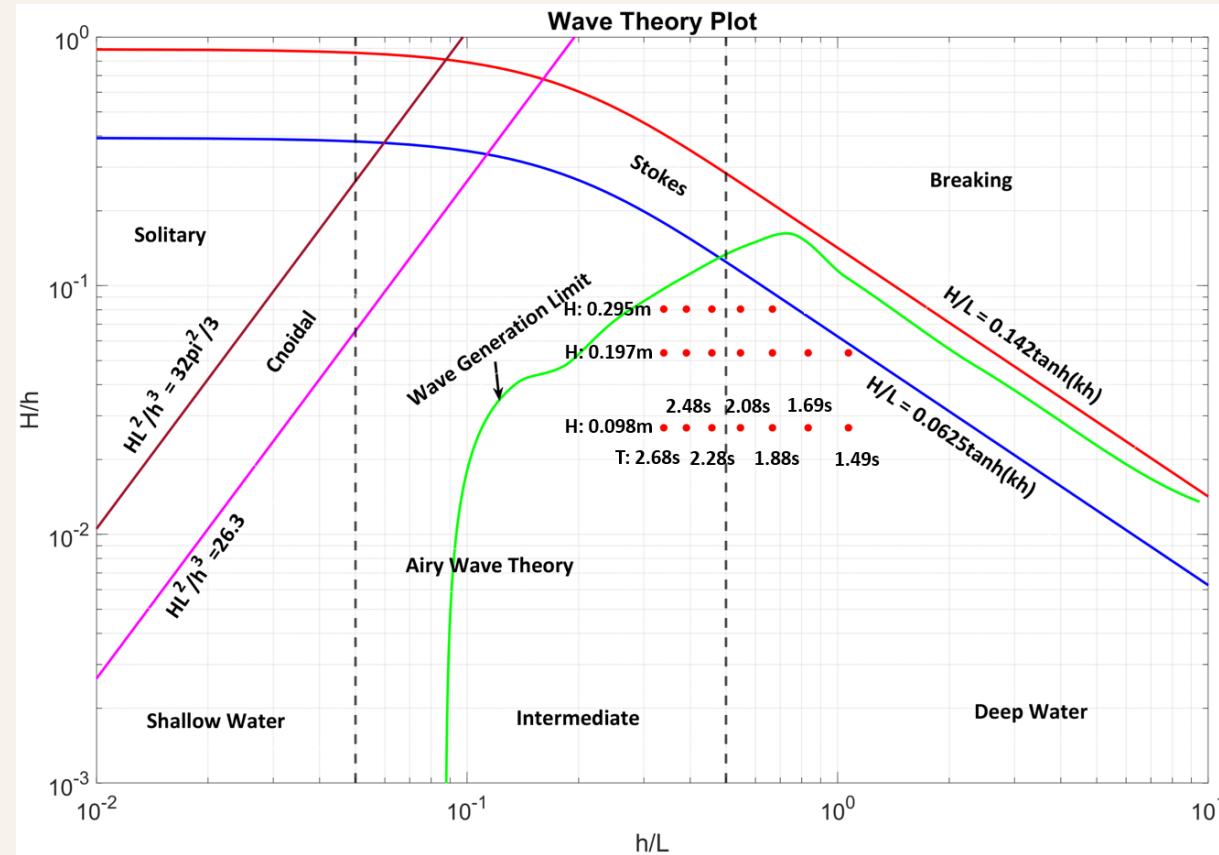
Corresponding field-scale wave conditions according to **water acceleration amplitude** matching criteria:

Wave height (m)	Wave periods (s)							
	7.5	8.5	9.5	10.5	11.5	12.5	13.5	
2.5	7.5	8.5	9.5	10.5	11.5	12.5	13.5	
5.0	7.5	8.5	9.5	10.5	11.5	12.5	13.5	
7.5			9.5	10.5	11.5	12.5	13.5	



Sea-state Histogram at the Targeted AUV Docking Site: U.S. PacWave Test Site

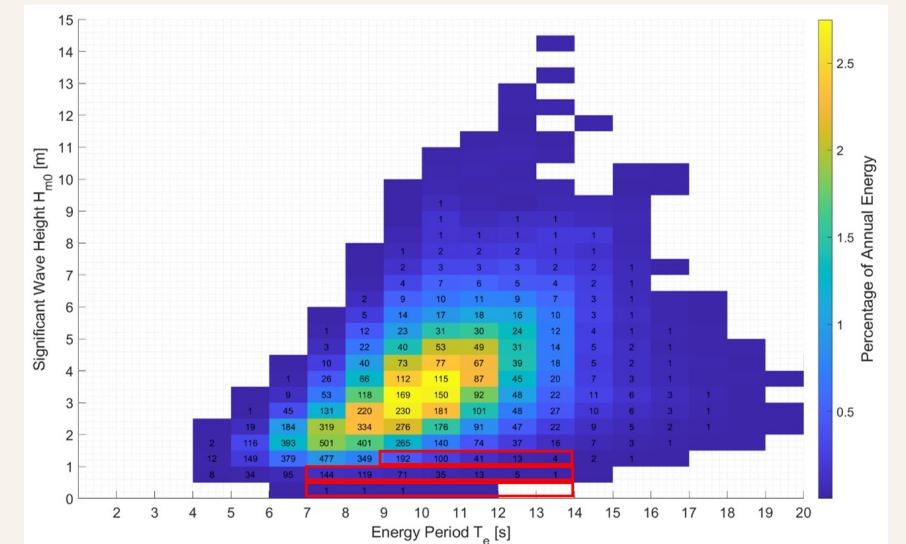
Model-Scale and Field-Scale Wave Conditions (velocity matching)



Selection Of Model-scale Wave Conditions Within the Wave Generation Limit
and Wave Breaking Limit

Corresponding field-scale wave conditions according to **water velocity amplitude** matching criteria:

Wave height (m)	Wave periods (s)							
	7.5	8.5	9.5	10.5	11.5	12.5	13.5	
0.5								
1.0	7.5	8.5	9.5	10.5	11.5	12.5	13.5	
1.5			9.5	10.5	11.5	12.5	13.5	



Sea-state Histogram at the Targeted AUV Docking Site: U.S. PacWave Test Site

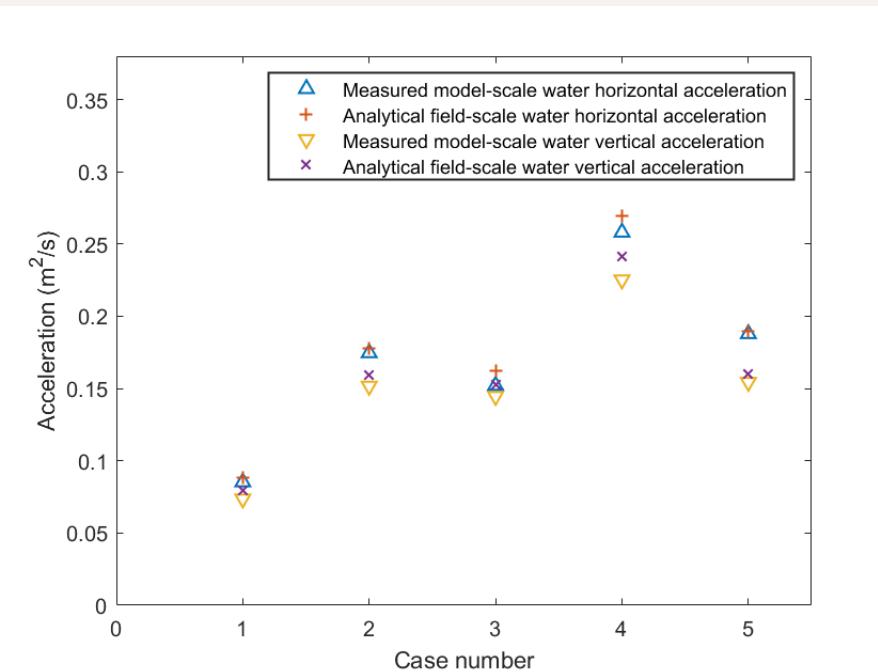
Validation of Wave Distortion Methods

- Five regular wave test cases were conducted in the laboratory to validate the wave distortion algorithms.

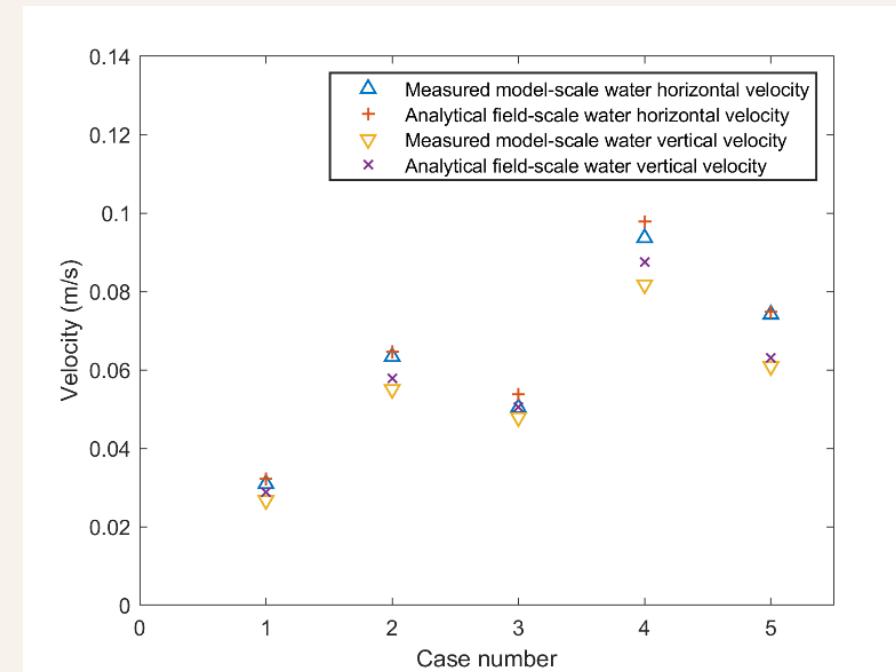
Case #	Model-scale regular waves		Field-scale regular waves for acceleration amplitude matching		Field-scale regular waves for velocity amplitude matching	
	Wave height (m)	Wave period (s)	Wave height (m)	Wave period (s)	Wave height (m)	Wave period (s)
1	0.098	2.28	2.488	11.50	0.494	11.50
2	0.198	2.28	5.028	11.50	0.998	11.50
3	0.198	2.08	5.028	10.50	0.998	10.50
4	0.298	2.28	7.567	11.50	1.502	11.50
5	0.198	2.48	5.028	12.50	0.998	12.50

Validation of Wave Distortion Methods (continued)

- Measured model-scale and analytical field-scale water particle acceleration and velocity in good agreements



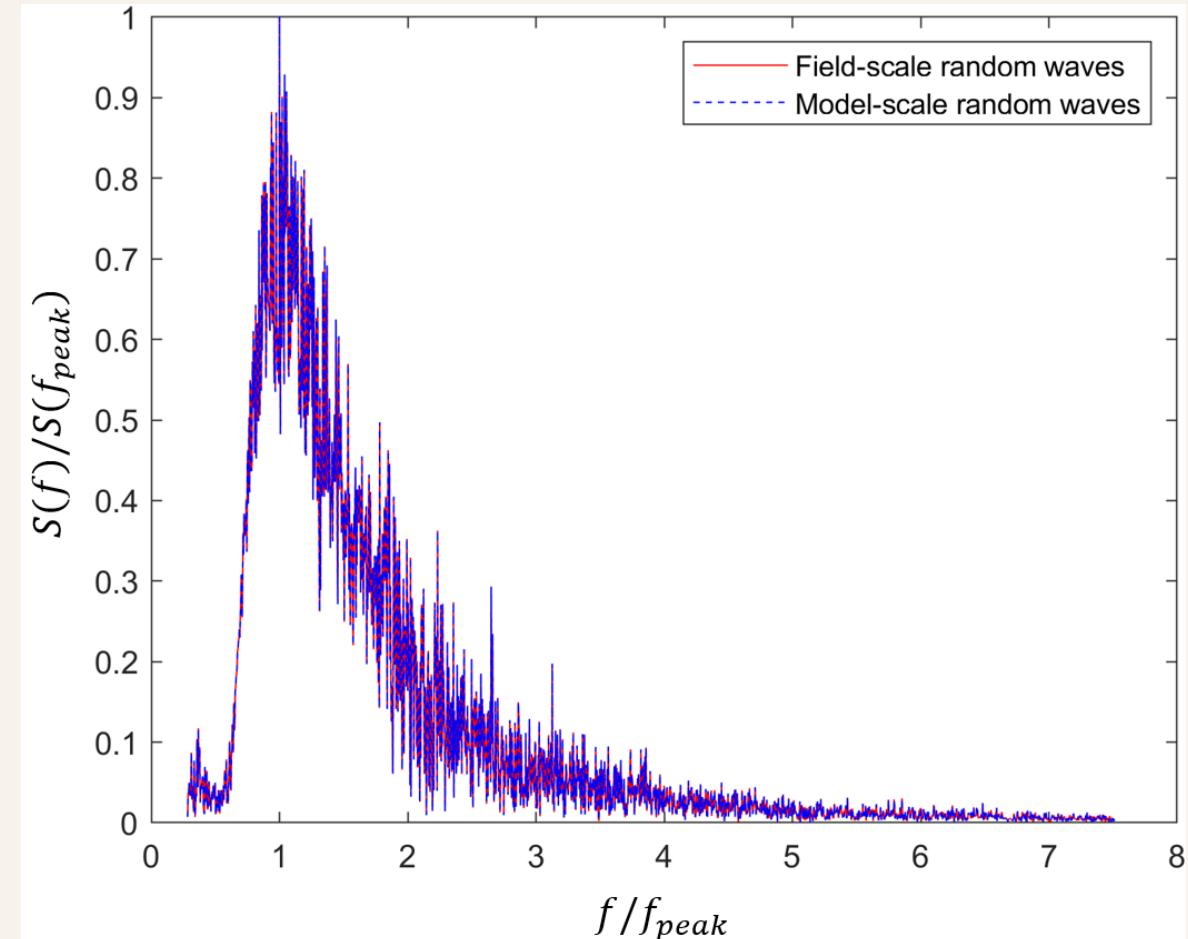
Comparison of water particle accelerations



Comparison of water particle velocities

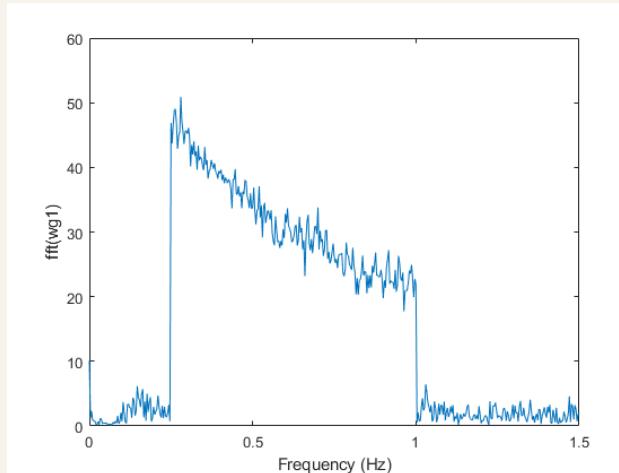
Random Wave Distortion Example

- Model scale random waves
 - $Tp=2.28\text{ s}$, $Hs=0.198\text{ m}$
- Field scale random waves (acceleration matching)
 - $Tp=11.5\text{ s}$, $Hs= 5.0\text{ m}$
- Model-scale random waves retain the same shape of power spectra density as the field-scale waves

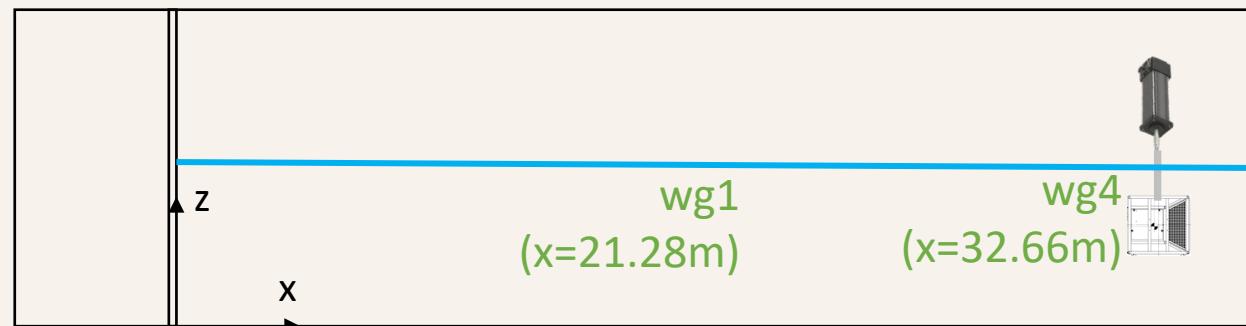


Validation of Wave Prediction Method

- Multi-sine waves
 - Wave period T (1 - 4 s)
- Wave gauge locations
 - Upwave wave gauge
 - Wave gauge at the dock
- Upwave time
 - 10 s (field scale) - \rightarrow 2 s (model scale)
 - 2.2 s from wg1 to wg4 under $T = 4$ s

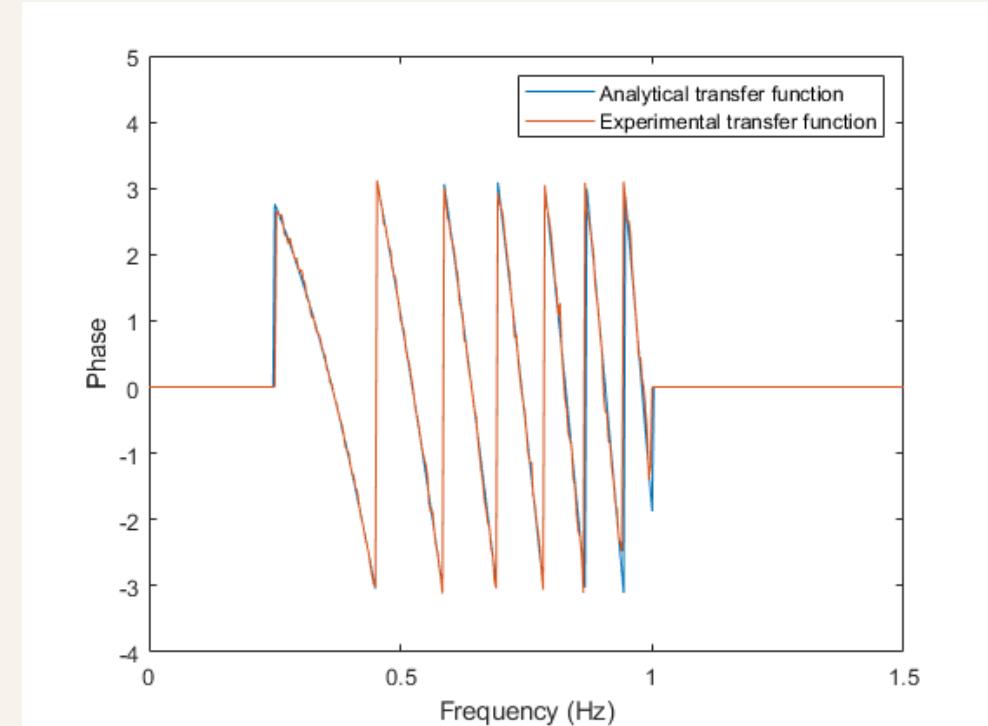
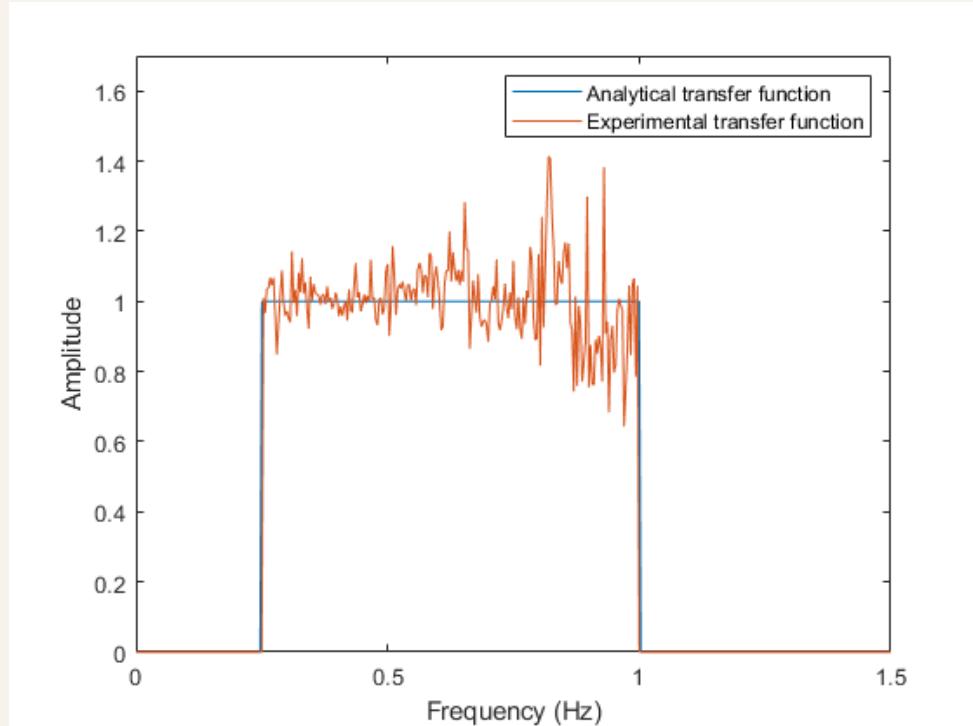


Wavemaker



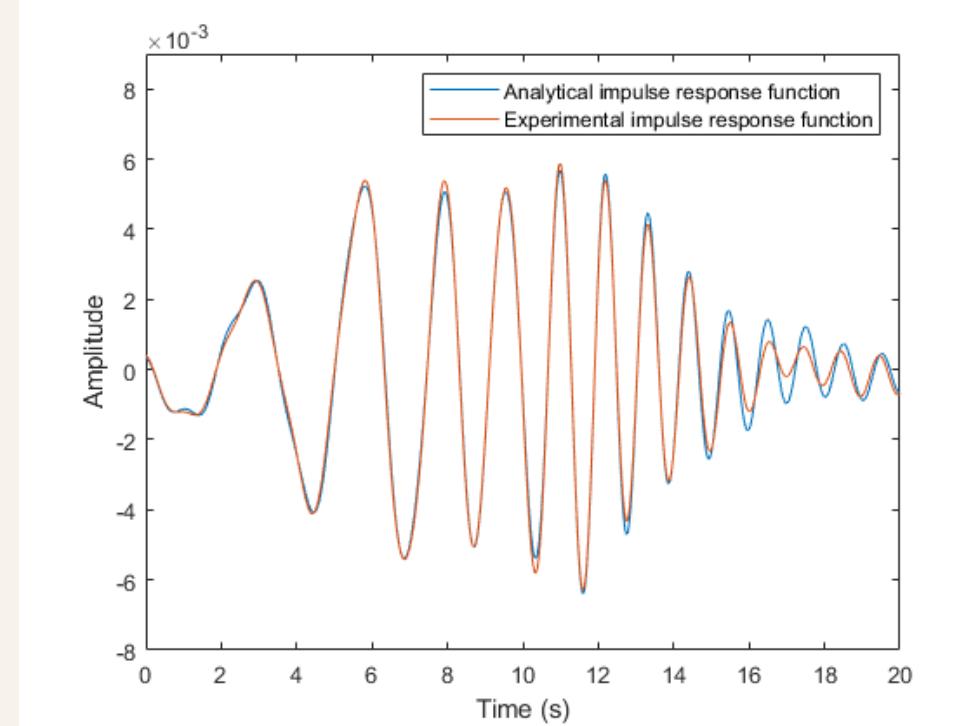
Validation of Wave Prediction Method (Continued)

- Frequency domain transfer function from upwave wave elevation to near-structure wave elevation



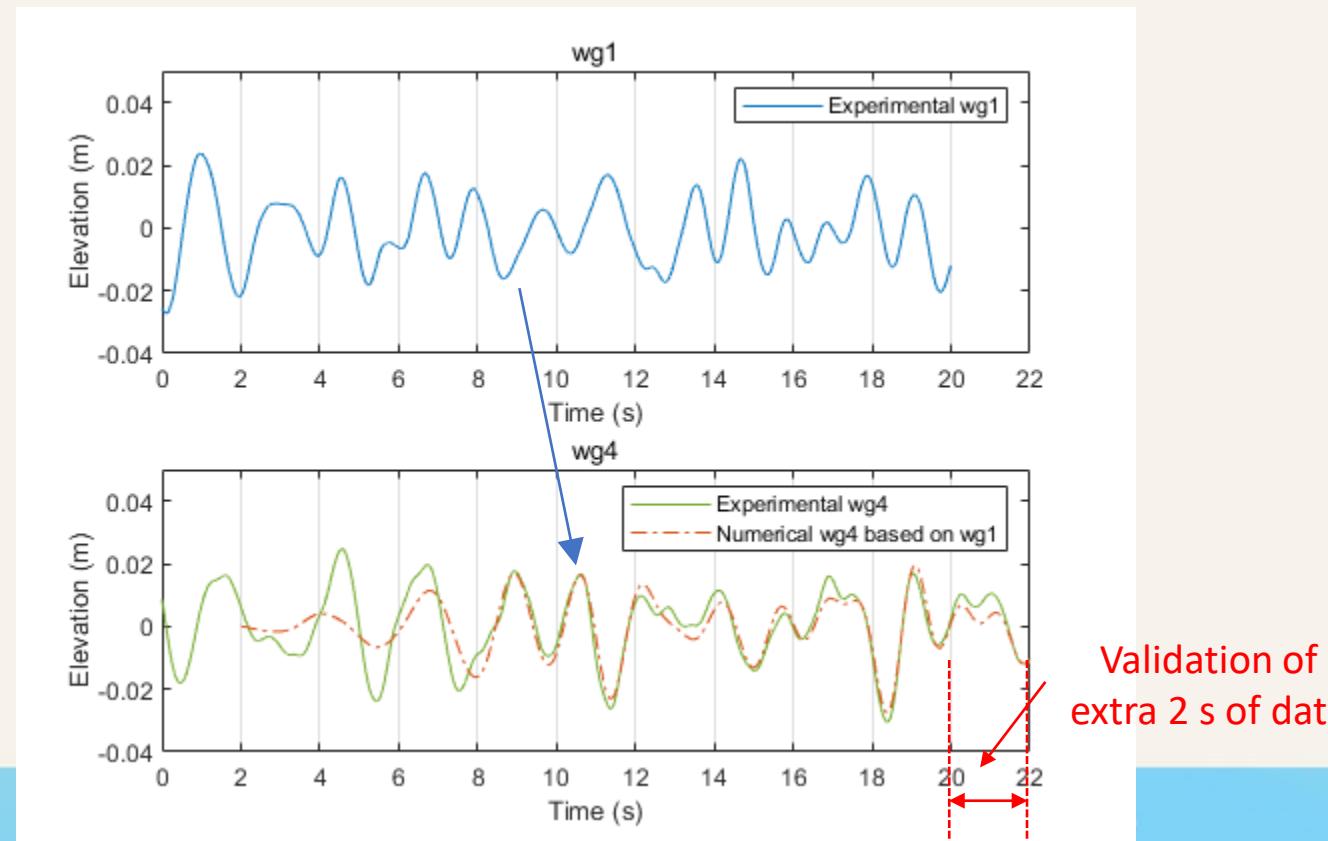
Validation of Wave Prediction Method (Continued)

- Time domain impulse response function from upwave wave elevation to near-structure wave elevation



Validation of Wave Prediction Method (Continued)

- The predicted wave elevation at wg4, based on wg1 wave elevation and impulse response, can provide extra 2 seconds of data



Summary

- 2024 WEC-AUV testing
 - Asynchronous testing
 - Validation of wave distortion method
 - Validation of wave prediction method
 - “Wave Distortion Methodology for Experimental Mixed-scale Testing of Underwater Vehicle Docking” OMAE Conference Proceedings 2025
- 2025 WEC-AUV testing (September 2025)
 - Real-time testing

Bryson Robertson (bryson.robertson@oregonstate.edu)

Junhui (Jason) Lou (junhui.lou@oregonstate.edu)

David Okushemiya (okushemd@oregonstate.edu)

p m e c .u s

Wave Force on AUV

- Wave-induced forces on AUV calculated by Morison equation:

$$F = \underbrace{\rho C_m V u_r}_{F_I} + \underbrace{1/2 \cdot \rho C_d A u_r |u_r|}_{F_D}$$

F_I is the inertia force, depends on water particle acceleration u_r

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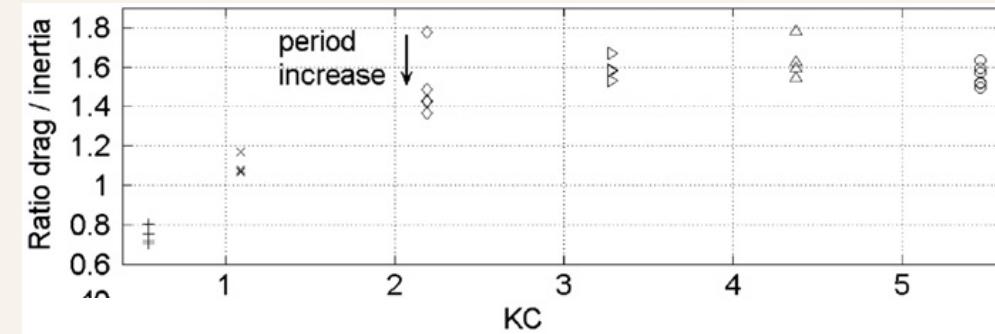
- The dominate wave force component is related to the Keulegan–Carpenter (KC) number

$$KC = UT/D$$

U is the maximum wave-induced particle velocity; T is the wave period; D is the AUV characteristic dimension

$KC < 1$: inertia force is larger than drag force

$KC > 1$: drag force is larger than inertia force



Avila, Juan Pablo Julca, and Julio Cezar Adamowski. "Experimental evaluation of the hydrodynamic coefficients of a ROV through Morison's equation." *Ocean engineering* 38.17-18 (2011): 2162-2170.