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 An Experimental Study of the Thrust and Power Produced by a 1/20th Scale Tidal Turbine Utilising Blade Winglets
 Rodolfo Olvera-Trejo ^{a*}, Luke E. Myers ^a, Luke Blunden ^a, AbuBakr S. Bahaj ^a
 ^a Faculty of Engineering and Physical Sciences. University of Southampton University Road, Southampton, SO17 1BJ, United Kingdom

8 Abstract

7

9

10 Winglets have been employed in the aviation industry to reduce vortices generated at aircraft wings, 11 decreasing drag, and hence increasing fuel economy. For rotating applications previous experimental 12 and numerical studies addressed the application for wind turbines and suggested winglets facing 13 backwards on the suction side of a blade could increase the power capture. This paper presents 14 experimental work using a scale 3-bladed horizontal axis tidal turbine. An oil-based paint flow 15 visualisation coupled to blade thrust and torque measurements helped to identify the mechanism 16 behind the phenomenon affecting the performance of winglets facing the suction side of a turbine 17 blade. The results show that on average a winglet facing downstream decreases the power 18 coefficient 1-2% and increases the thrust coefficient up to 6% for tip speed ratios 5.0-7.0. On the 19 other hand, a symmetrically mirrored winglet facing upstream increased the power coefficient by 1-20 2%, and the thrust coefficient by 3-4%. Further, increased bending moments at the root of the blade 21 were estimated to be in the range 4.5-6.0%. Winglets have the potential to provide a meaningful 22 increase to power capture at minimal additional capital cost without increasing rotor diameters. 23 Further work to optimise pressure-side winglets should be conducted.

24

26 27

25 Keywords: Experimental, flow visualization, marine energy, tidal turbine, winglets.

1. Introduction

28 Globally there are ongoing activities with targets geared to decarbonise our electricity generation. 29 Many countries have set targets to achieve an ever-increasing share of electricity production from 30 renewable energy sources to alleviate the emissions emanating from fossil fuel use. More recently 31 an additional- urgency to move to low -carbon sources was brought into sharper focus by global 32 geopolitical events – such as the war in Ukraine and its effect on gas supplies. Wholesale prices for 33 gas and electricity have increased sharply from relatively stable levels and national governments are 34 now taking security of supply much more seriously and as a driver to develop indigenous sources of 35 renewable energy electrical power generation. Previously, the EU Renewable Energy Directive [1] 36 set a target of 20% renewables by 2020 on average between member states which was recently 37 revised upwards to 45% by 2030 [2]. Similarly, the UK had a target of 30% of its electricity to be 38 produced from renewables by 2020 [1], which was achieved and exceeded in 2019, where 35% of 39 total electricity generation came from renewables. More recently, the UK announced an intention 40 of achieving 95% of its electricity from low-carbon sources by 2030, with high dependence on 41 offshore wind, solar energy, and nuclear power to support electricity supply independence and 42 security [3].

43

44 Marine energy, specifically that which arises from the kinetic energy of the flow in the oceans (tidal 45 stream and ocean currents), can contribute to renewable energy capacity, and increase diversity of

generation [4]. Tidal stream is also highly predictable so that power generation can be smoothly
integrated in power grids delivery at scale. However, as this is an emerging technology, it will need

^{*} Corresponding author. <u>R.Olvera@soton.ac.uk</u> Energy and Climate Change Division, Faculty of Engineering and Physical Sciences, University of Southampton, SO16 7QF, Southampton, United Kingdom.

48 clear support mechanisms to achieve a reduction in the presently high Levelised Cost of Energy 49 (LCOE) so that it can compete with other renewables [5].

50

51 At the time of writing and in many countries, the support for marine energy technologies is 52 somewhat uncertain. However, recently the UK Government has provided a ring-fenced funding 53 support mechanism for marine energy in its fourth round of the Contracts for Difference (CfD). The 54 CfD funding guarantees a fixed price for electricity from renewables supplied to the national grid. In 55 July 2022 under the UK CfD scheme, it was announced that four free stream tidal energy projects 56 with a total installed capacity of 40.82 MW, at CfD price of £178.54/MWh will be supported [6]. This 57 must be seen in the context of a historical market price of approximately £50/MWh since 2010 as 58 compared to 2022 where the level is currently in the range £150 to £250 /MWh as a result of market 59 price volatility. 60 61 There have been several deployments of sizeable tidal turbines to date with a latter move to small

62 grid-connected farms or arrays of multiple devices. The European Marine Energy Centre (EMEC) in 63 Orkney, UK, maintains grid-connected testing berths currently serving large-scale prototype devices. 64 The most advanced projects at the time of writing are the Shetland tidal array located in Bluemell 65 sound consisting of four 100kW devices and the Meygen project located in the Inner Sound of the 66 Pentland Firth presently consisting of four devices with total rated power of 6MW. There are 67 numerous areas in waters around the British Isles and indeed worldwide with consents and 68 permissions granted for freestream tidal energy projects. The €46.8m TIGER project funded by the 69 European Interreg programme has a stated aim to support the tidal industry to reduce costs from an 70 estimated €300MW/h to €150MW/h by 2025 [7] as well as provide support for up to 8MW of

71 installed capacity at sites around the Channel region between the UK and France.

72

73 Reducing the LCOE can be achieved by reducing the capital cost of the turbines in combination with 74 maximising power generation through increased efficiency of energy conversion that can arise from 75 optimising the power capture, power-take-off and electrical subsystems. One significant gain can be 76 made from the primary power-capture subsystem which in most cases for a tidal turbine is a lift 77 force-based rotor. Common routes such as increasing rotor diameter or constructing thinner more 78 slender blades are naturally limited due to the high thrust forces per unit area and the constrained

- 79 depth of tidal sites.
- 80

81 Winglets of different designs have been employed extensively in the aviation sector and now most 82 new modern commercial aircraft have winglets present at the wing tips. Enercon, to the best of the 83 authors' knowledge, is the only wind turbine manufacturer that has invested in research that has led 84 to winglets being used on its most recent designs [8]. However, to our knowledge there is no 85 available performance data is made available in the public domain. In implementing winglets to a 86 turbine blade, blade root and tip losses are two areas that will require attention with regard to 87 increasing power capture. Further, Enercon has recently deployed blades that extend onto the hub 88 nose cone (with flow-directing surfaces on the nose cone itself) to minimise hub losses and winglets 89 at the blade tips to minimise or even negate aerodynamic tip losses.

90

91 This work focuses on the design and quantification of performance of winglets installed on a 1-metre 92 diameter model tidal turbine. The work investigates the advantages of winglets for a tidal turbine to 93 increase power capture for the same rotor diameter through a blade modification that has a 94 relatively modest cost, thus reducing the LCOE with minimal change to the overall device design.

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2. Review of winglet design, application and research

Throughout the years, different methods have been proposed to increase energy extraction from 101 102 turbine blades using techniques such as: micro-tabs, non-straight blades, winglets, passively 103 adaptive blades, slots, and tubercles. The most widely studied type, and probably the ones that have 104 shown better results on aeroplane wings, are winglets. In 1897, the English engineer Frederick W. 105 Lanchester obtained a patent for vertical surfaces at the wing tips. In 1976 an aeronautical engineer, 106 Richard Whitcomb, conducted research at NASA using the term winglet to refer to a nearly vertical 107 wing extension in order to reduce the induced drag on wings [9]. In principle, the winglets' main 108 function is to prevent the interaction from the high to the low-pressure sides of the wing, reducing 109 the tip vortex, whilst decreasing the spanwise flow, resulting in reducing the induced drag [10]. 110 Figure 1 (Left) shows the vortex formed at the edge of a wing where the flow from the high-pressure 111 side travels towards the low-pressure side, as a result of the pressure difference. Figure 1 (Right) 112 illustrates the same vortices occurring at the turbine blade tips. In contrast to an aeroplane wing, 113 where vortices are perpendicular to the stream flow, for rotating turbines (wind or tidal), the 114 vortices travel in the same direction as the fluid.



115116Figure 1. Left: Vortex direction on an airplane wing. Right: Tip vortices on a tidal turbine.

117 Early work, in 1985 [11], which tested tip devices on a horizontal axis wind turbine found no 118 apparent improvement over the regular wing performance. The work emphasized that 'The 119 promising results obtained on nonrotating wings make it difficult to accept that tip devices could not 120 improve wind turbine performance'. Mie University, in collaboration with Delft University of 121 Technology (DUT), carried out a series of experiments on "Mie-type" winglets [12]. The "Mie-type" 122 vanes of approximately 20% of the height of the blade were tested and an increase in the power 123 coefficient (C_p) of around 27% for a blade Tip Speed Ratio (TSR) of 4 was reported. After that, Van 124 Bussel [13] developed a momentum theory for a blade-winglet configuration. The main assumption 125 was that the increase in power was due to the shift in the vorticity of the wake downstream. Further 126 experiments and an adjusted theoretical model were then reported showing a 17% increase in

- power coefficient for a tip speed ratio of 5. Other studies in 2003 were conducted and a power
 augmentation of 8.75% was reported [14].
- 129
- 130 Later in 2006/07 Johansen, Sørensen and Gaunna [15] used Computational Fluid Dynamics (CFD) to
- 131 investigate the possible increase in C_P by using winglets on wind turbines tested at Risø National
- 132 Laboratory, Denmark. A key aspect of their study was the utilisation of the geometry described by
- 133 Maughmer [10] which defined 8 key geometric parameters of winglets: height (relative to the blade
- 134 length), radius of curvature (relative to the winglet height), cant angle⁺, toe angle, twist, aerofoil,

⁺ As an unwritten convention, positive cant angles face the back of the turbine and negative ones to the front, The first ones have the same orientation as winglets on aeroplane wings.

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135 chord distribution and sweep (Figure 2). Their initial study using the general-purpose incompressible

Navier Stokes- solver EllipSys3D on winglets 1.5% (of blade length) high, a cant angle of 90°, and a
 sweep angle of 0° concluded that winglets could increase power coefficient by 1.3% while increasing

the thrust coefficient 1.6% for the best configuration, that winglets affect approximately the outer

139 14% of the blade, and that winglets facing downstream performed better. Further work by the same

140 group using the same solver, provided analyses of 10 winglets facing downstream, with heights

varying from 1-4%, curvature, radii 12.5-100%, twist angle up to 8°, and one with a sweep angle of

142 30°. They found an increase in power of around 1.2% to 2.8%, with an increase in thrust coefficient

- 143 (C_T) of 1.2% to 3.6% [16]. The study concluded that the power augmentation was a consequence of a
- reduction of tip effects, and not caused by the shift on downwind vorticity as it was believed until then. The idea that downwind winglets were superior was still supported. The studies were
- 146 conducted using a Free Wake Lifting Line code and the CFD Navier-Stokes solver EllipSys3D [17].
- 147





9 Figure 2. Winglet geometry design variables.

150

151 Over the last 15 years, more studies have been carried out, incorporating winglets of less than 10% 152 of relative height with respect to the blade length, resulting in power coefficient increases ranging 153 from 2% to 8%. Chattot [18] studied the effects of blade tip modifications on wind turbine performance using an optimization code, based on a numerical vortex model. The results favoured a 154 155 backward sweep, and forward dihedral and winglet (facing upstream), with a height of 10%, giving a 156 C_P increase of 3.5% at a TSR of 5.39. Lawton and Crawford [19] used a free wake vortex-based code 157 and concluded that a winglet facing downwind of a 5% height would result in a power increase of 2% 158 with a 2.8% increase in thrust. Elfarra et al. [20] used CFD to solve the Reynold saveraged Navier 159 Stokes (RANS) equations plus a genetic algorithm to optimize a winglet design of 1.5% height, 84° 160 cant angle, 2° twist, and no apparent radius of curvature. The estimated power capture increase was 161 9% and a 1.3% increase in the thrust coefficient. Subsequently, using the same computational 162 method, it was reported that winglets add aerodynamic forces and bending moments due to their 163 weight. Cant angles of 45° and 90° were analysed, with positive and negative sweeps. Within a TSR 164 range of 1.57.5, a 3.24.6 increase in power coefficient was estimated and 0.81.5 increase in thrust 165 coefficient [21].

166

167 Gertz and Johnson [22] experimentally set a wind turbine baseline case for exchangeable tip designs

168 for a 3.3 m diameter turbine. Then two winglet designs were evaluated, of 8% height, 90° cant angle,

- and -0.5° twist. The study showed a power increase of 5%-7% at a TSR of 6.7. Both winglets were
- 170 found to have a bell-shaped power curve [23]. In a different experiment, the interaction between

- 171 two wind turbines fitted with winglets was studied. The wind turbine located downstream saw a
- decrease in the power capture, however, the added power extraction of both was higher. Winglets
- had a height of 6%, 90° cant angle, 1° twist, and -0.5° sweep angle. The increase in power coefficient
 recorded was 4.2% at around a TSR of 6 and a 6.5% increase in thrust coefficient [24].
- 175

176 Mühle *et al.* [25] tested the effect of winglets on the tip vortex and the near wake, finding that for 177 wake regions larger than x/D=4.0, the wake's mean recovered faster due to the tip vortex 178 interaction stimulated by the winglets, in addition to a higher power extraction. Winglets were 179 designed with a height of 10.76%, a curvature radius of 3.09%, a cant angle of 90°, and a 17.86° 180 sweep angle. At a TSR of 6, the increase in power coefficient was 10.68% and 12.64% for the thrust 181 coefficient. The wind turbine manufacturer ENERCON is probably the only large manufacturer that 182 has exploited the potential of winglets. An example of this is the 2010 E-126 model, an upgraded 183 version of the 2007 E-126 model. The new model captured between 12% to 15% more energy by 184 refining the flow around the nacelle and by adding winglets [8].

185

186 Studies on winglets for tidal turbines are scarce, with most published work based on numerical 187 simulations. Most of the results produced a similar outcome that backwards-facing winglets should 188 perform better. Zhu et al. [26] took power and thrust measurements from an experimental study on 189 a horizontal axis marine turbine, carried out by Bahaj et al. [27] at the University of Southampton to 190 adjust their baseline for their RANS simulation. Their best simulated design produced a power 191 increase of 3.96% at a tip speed ratio of 7 and a pitch angle of 15° with a dual winglet of 2.5% height, 192 1.2% radius, 45° sweep, and each winglet facing the pressure and suction sides with cant angles of 193 90°. Ren et al. [28] proposed a triangular winglet bent downstream for their RANS equations 194 simulation. The results showed that winglets increased the power coefficient by 4.34% and the 195 thrust coefficient by 3.97% at an optimal TSR of 5. The design had a height of 6.3%, an 18:1 elliptical 196 tip of 10% the width of the winglet base aligned with the centreline of the blade, and a cant angle of 197 nearly 90°. In 2019, Ren et al. [29] also compared the effect of facing the winglets upstream and 198 downstream, finding that the best design achieved a 4.66% power increase when facing downstream 199 at a TSR of 4.2. The triangular winglets had a height of 5.3%, with a tip-to-base proportion of 84%, 200 and faced the suction side.

201

Young et al. [30] evaluated four different winglets, consisting of a linear extension of the tidal 202 203 turbine blade, varying the main parameter of cant angle. Two heights were considered, 10% and 204 20%, and relative curvature radii of 28% and 56% respectively. In their study, the power coefficient, 205 the hydrodynamic efficiency, and the structural efficiency were considered. After initial simulations 206 using a vortex lattice code called Tornado, three winglets were designed to face upstream, and one 207 downstream. In all cases it was hypothesized that blades with winglets perform better than the 208 regular blade. However, their results showed that only the winglets facing upstream did show better 209 performance. It was proposed that viscous effects (i.e., a separation at the corner of the blade-210 winglet junction) play a role in the reduction in power coefficient for the winglet facing downstream. 211 A summary of the aforementioned studies is given in Table 1, an expanded list can be found in [31].

212

213 Most recently, Bayu and Shin [32] investigated the effect of winglets on a wind turbine using a RANS 214 model coupled with a k- ω SST turbulence model. Their configuration included winglets facing 215 upstream and downstream directions. Their best design had a 3%R height and a cant angle of -90° 216 (upstream configuration) with power coefficient increases of 1-2% and thrust coefficient increasing 217 by 1-3%. Dejene et al. [33] used a similar model to investigate the effect of winglets on the NREL 218 Phase VI wind turbine. Winglets were 0.7% R high, facing the suction side and with cant angles of 30°, 219 45° and 60°. Expected power generation increase ranges from 5% to 10% with thrust coefficients 220 increasing 7% - 8%. Wang et al. [34] performed a numerical and experimental study of a tidal turbine with 10%R height and 60° bent winglet facing the direction of the current. The winglet configurationimproved the efficiency by 5.7% compared to the blade extension.

223

In summary, to date, there has been no consensus in the literature on the best direction of winglets
 for horizontal axis tidal turbine blades – upstream or downstream – let alone more detailed
 parameters such as height and curvature radius and their performance. This work is aimed at
 providing more insights into the performance of a model tidal turbine with rotor blades fitted with
 different winglets at different configurations tested experimentally.

229 230

3. Experimental design, setup and calibration

231 232 As part of this research, several winglets were designed, manufactured, and tested to provide an 233 understanding of the influence of varying winglet geometry on rotor thrust and power coefficients 234 as well as act as a benchmark for future work. The model turbine used in the experiments is a 3-235 bladed 'upwind' horizontal axis device with a blade diameter of 1m (Figure 3). The turbine is fully 236 instrumented and equipped with a dynamometer that measures rotor torgue and thrust at the hub. 237 It utilises full strain gauge bridges and runs 'wet' upstream of all seals and bearings [35]. Rotor speed 238 and blade radial position are quantified via a rotary encoder mounted on the main shaft within the 239 nacelle. A 2-stage planetary gearbox and a synchronous generator convert mechanical energy to 240 electrical and the rotor speed is controlled either by a wire-wound resistor bank or an electrical 241 variable load. All data travelling out from the turbine is sampled and amplified using a wireless 242 telemetry system to transmit data from the shaft to cables that join into a main umbilical cord that 243 also conveys the generated power out and low voltage DC power in to power the onboard systems. 244 Further details of the turbine design and general set-up can be found in [36,37]. The blade profile 245 geometry was provided by SIMEC Atlantis Energy Ltd. under an NDA, but a full tidal turbine blade 246 geometry can be found in [27]. The design was slightly modified to enable the tips to be 247 interchangeable, and the turbine has the capability to adjust the blade pitch from -5° to 5° in

248 increments of 1°.

249 Table 1 Studies on HATs with winglets and their design parameters

Research Paper				Parameters						Results		
Source	Туре	Country	Method	Height	Radius	Cant	T, t‡	Sweep	Aerofoil	TSR (λ)	P _{aug.}	T _{aug.}
				[%R]	[%H]	[°]	[°]	[°]			[%]	[%]
Wang <i>et al.,</i> 2023	Tidal	China	Exp. + CFD	10		60			S809	3.5 – 8	5.7	
Dejene <i>et al.,</i> 2023	Wind	Ethiopia	RANS k-ω SST	0.7		-90			S809	7.5	5-10	7-8
Bayu and Shin, 2023	Wind	Japan	CFD-RANS	1.5-5		-90,90			S809		2.21	2.02
Young <i>et al.,</i> 2019	Tidal	UK	VLM + Exp.	10, 20	(10 <i>mm</i>)	-90-90				4	10	
Ren <i>et al.</i> 2019	Tidal	China	CFD-RANS	5.3		-90, 90			NACA63-418	4.2	4.66	
Ren <i>et al.</i> 2017	Tidal	China	CFD-RANS	6.3	 C 	-75-90			NACA63-418	5	4.34	3.97
Zhu <i>et al.,</i> 2017	Tidal	China	CFD	2.5	48	-90, 90	-	45	NACA 63-812	3 - 10	3.96	
Ostovan and Uzol, 2016	Wind	Turkey	Exp.	6	(0)	90	1T	-0.5	PSU 94-097	~6	4.2	6.5
Elfarra, Sezer-Uzol and Akmandor, 2015	Wind	Turkey	CFD + GA	1.5	(0)	45 <i>,</i> 90	0, 2T	+ -	S809	1.5-7.5	3.2-4.6	0.8- 1.5
Lawton and Crawford, 2014	Wind	Canada	CFD	5		90	6.73T	0	NACA 64		~2	2.8
Elfarra, Sezer-Uzol and Akmandor, 2014	Wind	Turkey	CFD + GA	1.5	(0)	84	2Т		S809		~9	~1.3
Gertz, Johnson and Swytink-Binnema, 2012	Wind	Canada	Exp.	8	(0)	90	-0.5T	0	PSU 94–097	6.7	5-7	
Chattot, 2009	Wind	USA	Num.	10	(0)	-90			S809	5.39	3.5	
Gaunaa and Johansen, 2007a	Wind	Denmark	Num.	2	25	90			Risø B1-15	8	2.47	2.61
Johansen and Sørensen, 2007	Wind	Denmark	CFD	2	20	90	4T	0			1.0-1.8	1.2-
Johansen and Sørensen, 2006	Wind	Denmark	CFD	1.5		90		0	NACA 64-518		1.3	1.6
Shimizu <i>et al.,</i> 2003	<i>a et al.,</i> 2003 Wind Japan Exp. 9 Mie-type		type		NACA 4418	5.42	8.75					
van Bussel, 1990	Wind	Netherlands	Num.	20		Mie-type			NACA 4412	8	=	
Shimizu <i>et al.,</i> 1990	Wind	Japan	Exp.	~20		Mie-type			FX74-CL6-140	4	27	
Gyatt and Lissaman, 1985	Wind	USA	Exp.	5		Single, fin, and double			NACA 23012,21		-	

[‡] T: twist, t: toe angle



Figure 3. Turbine installed in towing tank (Top left), main blade (Top right), blade and winglet interface (Bottom left),
 3D printed winglets (Bottom right).

The blades were milled on a 5-axis CNC machine at the Engineering Design and Manufacturing Centre at the University of Southampton from T6082-T6 aluminium alloy, with an accuracy of ± 50 microns. The winglets were 3D printed in aluminium at an accuracy of ±0.1 mm, hand polished and finished.

257

The thrust and torque signals were collected at a frequency of 67 Hz, filtered and amplified via a wireless telemetry system located inside the nacelle. A National Instruments[®] data acquisition (DAQ) box, model NI USB-6210, would receive the analogue signals, pass them to a LabVIEW[®] program for real-time viewing, and save the data for post-processing. The power was dissipated either by using an Aim-TTi LD300 Electronic Load or a 280-W rheostat.

263

264 The thrust dynamometer was calibrated from 0 to 150 N at intervals of 30 N with a precision of 265 0.05 mN. The torque dynamometer calibration ranged from 0 to 11 N·m using intervals of 2.2 N·m 266 measured to 0.02 mN·m, by hanging 0.5 kg weights at 0.442 ±0.001 m from the centre of the shaft at 267 $0 \pm 0.5^{\circ}$ at the plane of rotation. The zero reading for the thrust has scattered noise with a normal 268 distribution as shown in the perpendicular histogram of Figure 4 with a standard deviation of 269 ±5.77 mV. The linear correlation has a value of 0.9999938 as shown in Figure 5. Measurement 270 uncertainties are shown in Table 2. Precision has to do with the instrumentation and the regression 271 uncertainty is derived from the calibration plot.

272





273274 Figure 4. Noise in the acquisition signal

274

276



277 278

78 Figure 5. Thrust calibration.

279 Table 2. Measurement uncertainties

	Thrust (N)	Torque (N·m)	Ω (rmp)	Power (W)
Precision uncertainty	0.8538	0.0327	0.48	0.49
Regression uncertainty	0.4311	0.0257	-	-
Total uncertainty	0.9564	0.0416	0.48	0.49
Percentage of the mean	1.29%	0.77%	0.53%	1.30%

280

281 Averaging the signal over a period of 120s and plotting the error, the mean and the standard

deviation converge with an error of less than 0.1% in just under five seconds as can be seen in Figure

6. After performing the repeatability test, it was found that the revolutions per minute (rpm) can be

estimated around a predefined value with an accuracy of ±0.48(02) rpm.

285



286287 Figure 6. Percentage error for a sample time of 2 minutes

288 Experiments were conducted at the wave/towing tank at Solent University in Southampton, UK. The 289 tank has dimensions of 60 m long \times 3.7 m wide \times 1.8 m deep. The turbine was towed at 0.76 m/s, 290 allowing the turbine rotor to rotate within the range of 60-120 rpm. The towing speed was selected 291 to give a sufficient range of blade Tip Speed Ratio whilst being slow enough to maximise data 292 collection at a fixed acquisition frequency. The Froude number was approximately 0.137 (water 293 depth 3.5m, velocity 0.76 m/s), scaled to be representative of a real tidal channel and Reynolds 294 numbers of approximately 1.5×10⁵ were observed at the tips of the blade (chord at scaled model of 295 0.0413 m) at an optimum rotational operation speed (TSR = 5). Towing faster resulted in minimal 296 change in performance curves (Re. independence), whilst decreasing time for data collection due to 297 length restriction. Depending on the winglet configuration, the rotational speeds chosen to 298 characterise the turbine were equivalent to values ranging from 4.5 to 7.5 TSR (λ). 299

The following standard equations are used to present non-dimensional rotor performance:301

$$C_{P} = \frac{Power}{\frac{1}{2}\rho Au^{3}}$$
Equation 1.

$$C_{T} = \frac{Thrust}{\frac{1}{2}\rho Au^{2}}$$
Equation 2.

$$TSR(\lambda) = \frac{\omega R}{u}$$
Equation 3.

302 Where ρ is the fluid density, *A* is the swept area of the rotor, *u* is the inflow velocity, ω is the 303 rotational speed in radians per second, and R is the rotor radius.

304 The characterisation of the turbine with the straight blade extensions (no winglets) for TSR from 4.5

to 7.5 is shown in Figure 7. The average value of C_P is 0.42, and C_T is 0.78, both values quoted for

306 further comparisons with winglets tests. Each TSR data point was obtained over a 1-min run to

307 characterise the performance of the blades with winglets. Each run has a ramp-up period and a

308 breaking period. In between these, a steady condition was achieved for approximately 30 seconds 309 which generated over 2,000 data points at a sampling rate of 67 Hz. The error bars are calculated





311 312 Figure 7. Tidal turbine C_P (Top) and C_T (Bottom) curves vs. TSR.

The maximum value of $C_{\rm P}$ is defined by the limit quantified by Betz [38] for a horizontal axis turbine 313 which is equal to 16/27 or 59.3% of the available power to the swept area of the rotor. In practice, 314 315 C_p is used as a global or whole-device efficiency value and is applied at the rear of the turbine incorporating electrical and drivetrain losses but here it is applied at the rotor and can be measured 316 317 using the dynamometer at the hub. Tip and hub losses are significant contributors to the difference between real rotor C_p and the Betz limit [35]. Figure 8, from formulae published by Wilson et al. 318 319 (1976) [39], illustrates the effect of tip losses on rotor performance and thus efforts to reduce blade 320 drag by minimising or completely eliminating tip losses that should be incorporated into the blade 321 design.







326 The design parameters of the winglets presented herein can be seen in Table 3. The three main

327 parameters that could be compared between winglets were height, radius of curvature, and cant

328 angle, plus aerofoil orientation (Figure 9). A positive cant angle means that the winglet is facing the

329 suction side (backwards) and a negative angle that is facing the pressure side (forwards). In this

330 study the only winglet facing the front of the turbine is winglet 7. In all cases, the distance from the

hub centre to the outer part of the blade is kept at constant 0.5 m.

332

333 Table 3. Design parameters for selected winglets – see also Figure 9..

-	Element	Height	Radius	Cant	Aerofoil	
-	Blade tip (T1)	0 mm (0.0%)	0%	0°	Blade	
	Winglet 2 (W2)	12.5mm (2.5%)	50%	90°	Extension	
	Winglet 3 (W3)	25 mm (5.0%)	50%	90°	Extension	
	Winglet 4 (W4)	50 mm (10.0%)	50%	90°	Extension	
	Winglet 5 (W5)	25 mm (5.0%)	25%	90°	Extension	
	Winglet 6 (W6)	25 mm (5.0%)	100%	90°	Extension	
	Winglet 7 (W7)	25 mm (5.0%)	25%	-90°	Extension	
	Winglet 8 (W8)	25 mm (5.0%)	25%	90°	Inverted	
2					W3	1
	W4		N5		W6	
	W7				W8	
						1



336 configuration as W5 as well but an inverted aerofoil which makes it a mirrored winglet to W7.



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341

3393404. Results and discussion

342 4.1 Winglet height

The first parameter to compare was winglet size. W2, W3 and W4 have a 2.5%, 5% and 10% height respectively, with a relative curvature radius of 50% (Figure 10).

345



Figure 10. Winglets 2, 3 and 4 (Table 3) with 2.5%, 5% and 10% height respectively with curvature radius of 50%.

347



348ISR349Figure 11. Winglet performance in terms of C_P and C_T as a function of TSR, height and comparison with straight blade, all350with relative radius curvature of 50%.

351 Figure 11 shows the winglet blade performance in terms of power (C_P) and thrust (C_T) coefficients for different heights (Table 3) as a function of TSR. W2 has an average C_P value of 0.40, whilst W3 and 352 353 W4 had C_P at 0.35 and 0.38 respectively. These values are lower when compared with a straight 354 blade. Additionally, in all three cases, the thrust coefficient increased when compared with a straight 355 blade. This was contrary to the assumption that the reduction in induced drag during turbine 356 operation could outweigh the increase in profile drag due to the addition of winglets [20]. 357 As can be seen in Figure 11, in terms of power coefficient (C_P) in all cases, the blade -winglet 358 configurations underperform compared to the straight blade. These results are in contrast to 359 previously published numerical studies on wind turbines [16,17,19], as well as the experimental 360 results from Ostovan and Uzol [24]. Computational simulations, specifically on tidal turbines, either

- 361 supported backwards-facing winglets or found no considerable difference regarding their
- 362 orientation, either facing forwards or backwards [26,29].
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- 364
- 365
- 366 367





380 Figure 12. Side view of winglets with same height, blade length and different curvature radii.

381 Figure 13 depicts the winglet performance in terms of C_P and C_T as a function of TSR, curvature and 382 comparison with straight blade, all with different radii and at height of 5%. It can be seen from the figure that varying the radius of curvature from 25% to 50% C_P has almost identical values of 0.36 383 384 (W5) and 0.35 (W3) respectively. Whilst W6 at a 100% radius gave a relatively higher value of C_P of 385 0.39. In terms of C_P, all winglets still underperformed versus the straight blade. Previous studies 386 compared the influence of the radius on the power coefficient [16,17], favouring a curvature radius 387 of around 25%. At the design stage, the various winglets were designed with heights up to 10% and curvature radii between 20% and 50%. In this experiment, winglets with different curvature radii did 388 389 not increase the power coefficient either, and there was no evident trend found as radius increased. 390



391TSRISR392Figure 13. Winglet performance in terms of C_P and C_T as a function of TSR, curvature and comparison with straight blade, all393with different radii and 5% height.

394 4.3 Winglet cant angle

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The third parameter to compare is the cant angle between W5 and W7 (Figure 14). The design of W7 was initially carried out for completeness, as most previous studies had favoured backwards-facing winglets. In fact, it turned out to be the first winglet with an evident difference in C_P, even presenting a higher C_P than the straight blade at some regions, and eventually being key to understanding other winglets' unexpected behaviour.



401 Figure 14. Winglets facing opposite sides of the turbine, where W5 is facing the suction side and W7 towards the pressure 402 side.



403 404 Figure 15. Power and thrust coefficient versus TSR for winglets facing opposite sides of the rotor showing the forward-405 facing winglets improving C_P over backward-facing winglets and straight blade in some regions.

406 Figure 15 (Left) shows a significant difference between the power coefficient of W5, of 0.36 on

407 average (facing the suction side), and W7 with a value of 0.42 on average (facing the pressure side),

408 except from TSR 6 to 7 where there was an increase of 1-2%. At the same time, both thrust

409 coefficients have an average value of 0.80 and have higher values than those of the straight blade.

410 In this work, W7 presented the first winglet to show an increase in performance than the straight

411 blade (Figure 15). It has the same geometry as W5, but it is bent upstream towards the high pressure

412 side of the blade. The first assumption to explain this behaviour is that when winglets are bent to the

413 back of the rotor, the aerofoil ends up being upside down (Figure 16). It is assumed that an aerofoil

414 rotating with such orientation would have more resistance to motion than one in an upright

415 position.









To compare the assumption made in the previous section, winglet W8 can be analysed. Its geometry

421 is bent towards the back of the turbine as W5, with an inverted aerofoil. With such a configuration,

the winglet ends up having a symmetrically-mirrored shape as W7 (Figure 17).



Figure 17. Aerofoil orientation for W5, W7 and W8.



428 429

429Figure 18. C_P and C_T curves versus TSR for opposite cant angles. W7 is bent towards the front, while W5 is bent towards the430back, by doing so, the aerofoils end up inversed to each other. Winglet 8 is similar to W5, with an inverted aerofoil, so it has431the same orientation as W7 that is facing the front. This allows a direct comparison between cant angles for winglets facing432opposite directions, as the aerofoil on both W7 and W8 have the same spatial orientation.

Figure 18, shows the results of changing the aerofoil orientation to allow a more significant comparison for the cant angle. The average C_P value of W5 is 0.36, W8 0.37 and W7 0.42. All winglets had an average C_T of 0.80. So, the difference in average C_P between W7 and W5 with opposite cant angles cannot be solely attributed to aerofoil orientation. Previous studies suggested that winglets facing the pressure side performed better than the ones oriented towards the suction side, Chattot [18] with an optimization code based on a numerical vortex model, and Young [30] using a vortex lattice method.

440

4.5 Surface flow visualisation

441 442

Following the quantification of rotor power and thrust performance, an oil-based paint flow 443 444 visualisation technique was used to study the flow on the surface of the winglets near peak C_P at a 445 TSR of 5.0 to visualise the flow on the surface of the two symmetrical winglets W7 and W8 facing 446 opposite directions, looking for an explanation on why W7 facing the front had a better performance 447 than W8, which is geometrically mirrored but facing towards the back of the turbine. An example of 448 the technique can be seen in [40]. In these experiments, oil-based paint was combined with flaxseed 449 oil, and by trial and error a dilution ratio of 2:1 was found to have the right viscosity for a TSR of 5. 450 Under normal testing the rotor was artificially started to overcome starting torque which resulted in 451 a peak RPM greater than steady operation. For the runs with flow visualisation the starting 452 procedure was modified to ensure the maximum and steady RPM only occurred during the steady 453 operation period. Figure 19 (Left) shows a normal test run where the carriage acceleration produces 454 a spike in the turbine speed. Figure 19 (Right) is the plot of the modified run to avoid such abrupt 455 increase. It can also be noticed that the time to reach a steady speed almost doubles, steady speed 456 time lasts less than in a normal run (as no data is processed), and instead of a gradual stop of the 457 carriage, the turbine is left to stop on its own







460 As can be seen in Figure 20 (Left), it was identified that the phenomenon behind the 461 underperformance of all winglets, except W7, was a vortical flow structure being formed at the 462 blade-winglet interface. The schematic of the vortex is shown in Figure 20 (Centre), produced by a 463 large flow detachment from the surface. The same behaviour was found in all winglets facing the 464 suction side (Figure 21). That is what was impeding the winglets from enhancing the power capture 465 and in fact reducing the power coefficient compared to a straight blade. However, in the case of W7, 466 there was no such vortex found as can be observed in Figure 20 (Right). All photographs were captured immediately after each run by bringing the turbine out of the water and removing the 467 468 winglets. 469



470 Figure 20. Oil-based paint flow visualisation of a vortex behind winglets facing the suction side (Left), vortex
471 schematic (Centre), and no vortex towards the pressure side (Right).

472





474 Figure 21. Oil flow visualisation for T1 and the rest of the winglets facing the back (suction side).

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483 484

Judging from Figure 21, the difference in the performance of backward-facing winglets is attributed to vortices that vary in shape and size, not only per configuration but most probably for the same winglet at different speeds. Taking W2, W3 and W4, it can be seen that as the winglet increases in size, so does the vortex, with the difference that W3 and W4 seem to have either a split vortex or two of them. The more pronounced radius of curvature seems to be responsible for such an effect. A better understanding of the vortices could be achieved by using flow visualisation in 3D that includes the flow away from the winglet surface.

5. Conclusions

In recent years, numerical simulations using CFD have sought to predict the effect that blade tip winglets might have on the power and thrust coefficients of horizontal axis wind turbines. Such predictions suggested that the addition of winglets could increase the power coefficient in a range from 2% to 8%. The three main design parameters varied were height, curvature radius and cant angle. Winglet heights of up to 10% had been favoured, with relative curvature radii of around 25% and up to 50%, and a cant angle of 90° (facing the suction side). Until now only disparate experimental work has been conducted and very few studies concerning tidal turbines.

This work presents a series of experiments using a 1m-diameter 3-bladed horizontal axis tidal turbine equipped to measure rotor thrust, torque, rotational speed, and blade position. A range of winglet designs were manufactured and tested to quantify the effect of varying winglet height, radius, and cant angle. It was found that all winglet geometries tested that faced the suction side of the blade decrease the power coefficient compared to a reference straight blade. With the use of an oil-based paint flow visualisation, it was possible to identify vortical flow structures and areas of flow

- 498 separation where winglets interface with the tip of the straight portion of the blade; Features that499 are unlikely to be simulated using inviscid numerical models.
- 500 An increase in power coefficient of 1-2% was measured for a symmetrical winglet facing the 501 pressure side of the blade together with an increase in the thrust coefficient of up to 3-4%.
- 502 The addition of winglets could provide meaningful increases in power capture for a marginal
- 503 increase in capital cost with no additional increase in rotor diameter. Adding winglets might be more
- 504 favourable than increasing rotor diameter to increase power as the latter brings blades into closer
- 505 proximity with sheared flow close to the seabed and wave motion near the surface and the resultant
- 506 increase in dynamic loading.
- 507 This work quantifies the performance of a range of winglet designs and gives some insight into why
- 508 certain designs located on the suction side of the blade underperform compared to previous
- 509 numerical simulations. Numerical models that can simulate and more accurately quantify the effects
- of rotational flow and separation are recommended for any continuing work in this area. This work
- also provided some experimental evidence of enhancements of performance and to this end, further
- 512 work is being planned to expand the range of winglets that can be used and to explore additional
- 513 geometric properties including winglets orientated upstream on the pressure side of the blade.

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521 Data Availability

- 522 Datasets related to this article can be found at <u>http://dx.doi.org/10.5258/SOTON/D2129</u>, hosted at
- 523 ePrints Soton (Olvera Trejo, Rodolfo (2022) Winglets. University of Southampton).

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Declaration of interests

☑ The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

□ The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

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