

Comparison of experimental and BEM heave excitation forces for contrasting float geometries

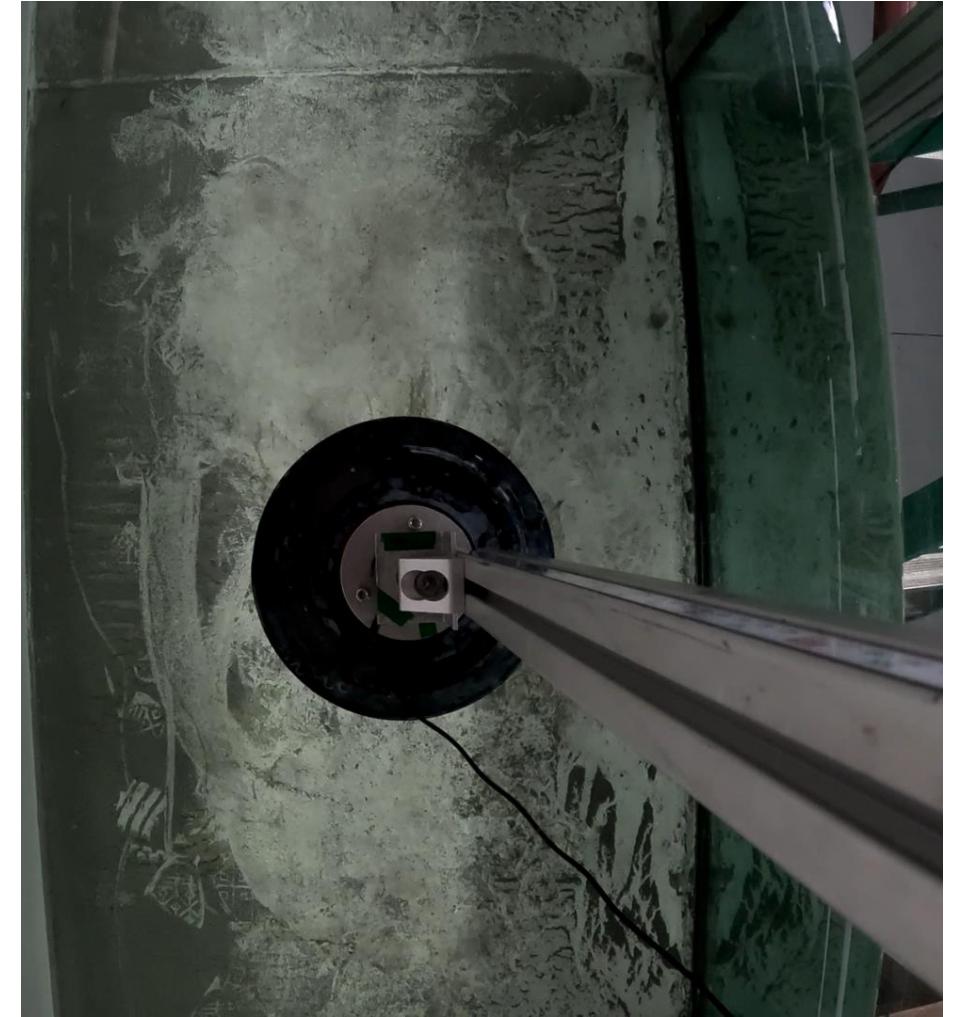
Sarah May Palmer,
Sadie Kass, Curtis Rusch, Brittany Lydon,
and Brian Polagye



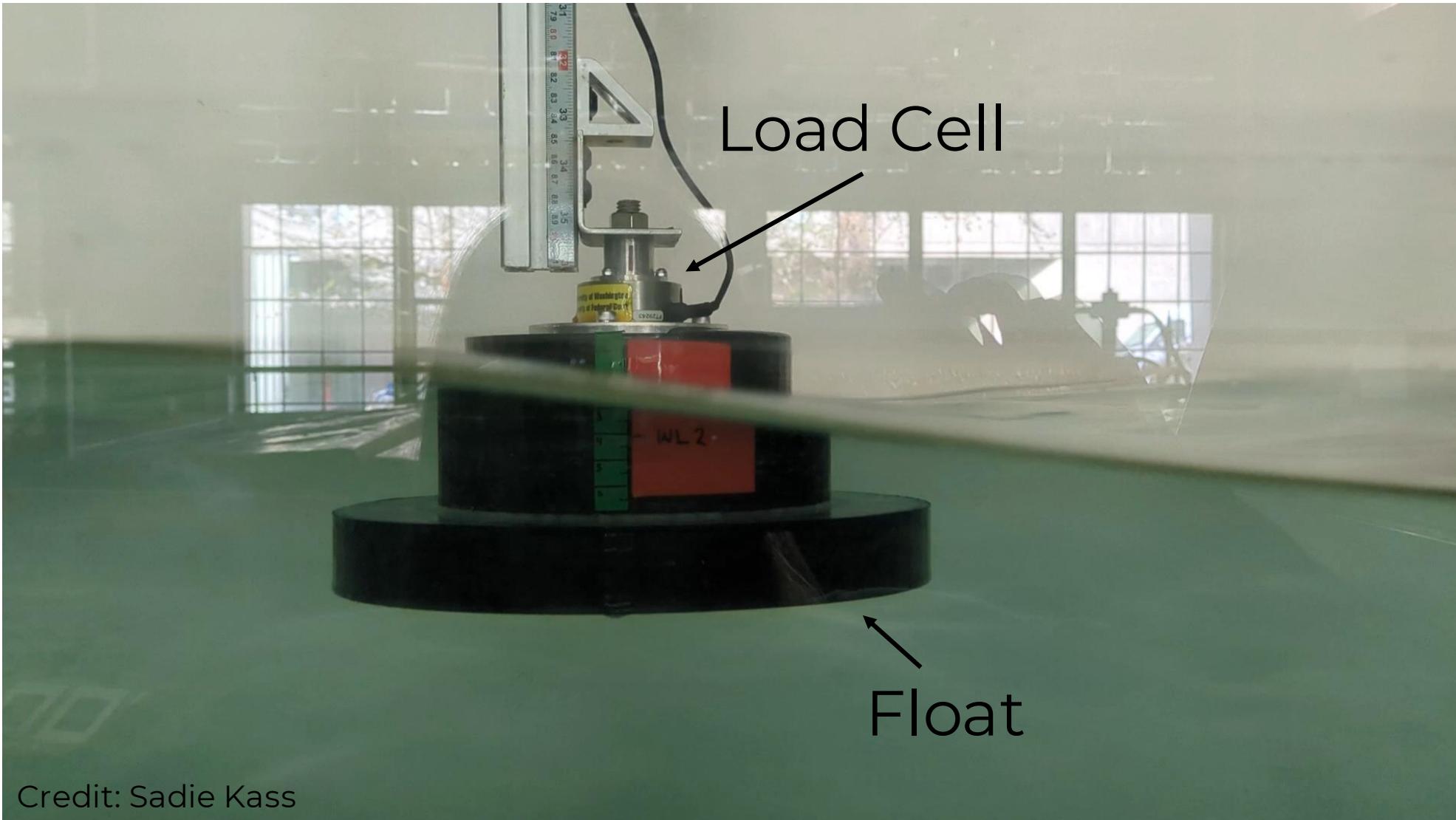
Project Goal

Boundary-Element-Methods (BEM) are widely used in WEC design

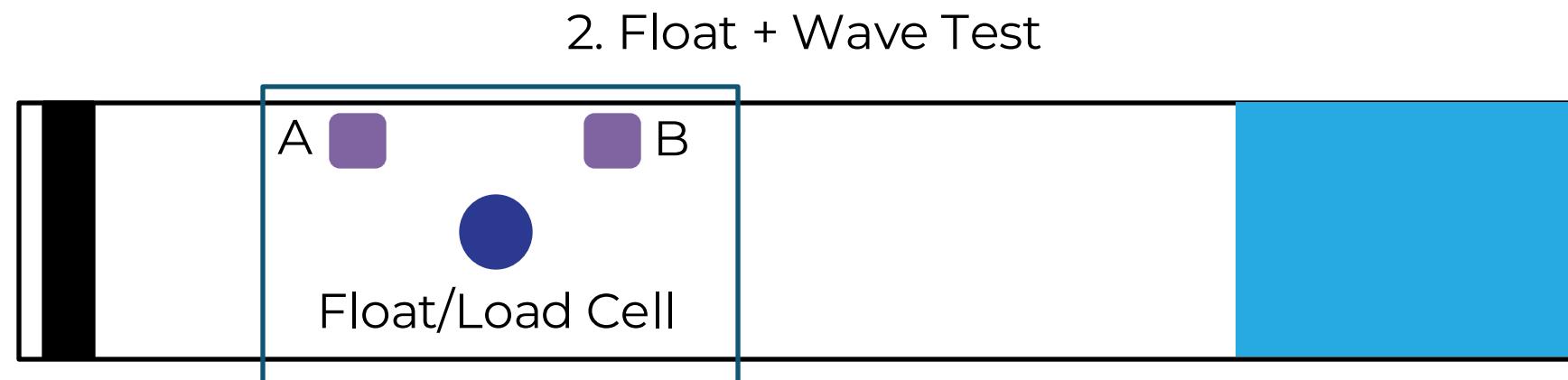
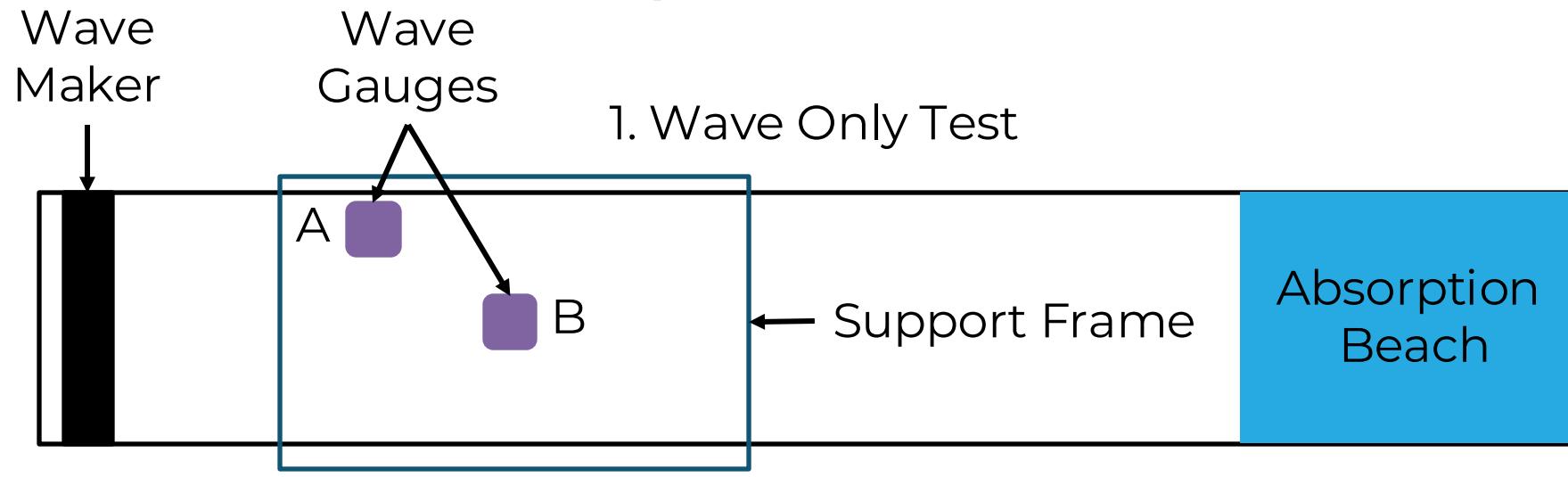
How accurate is BEM for more complex float geometries?



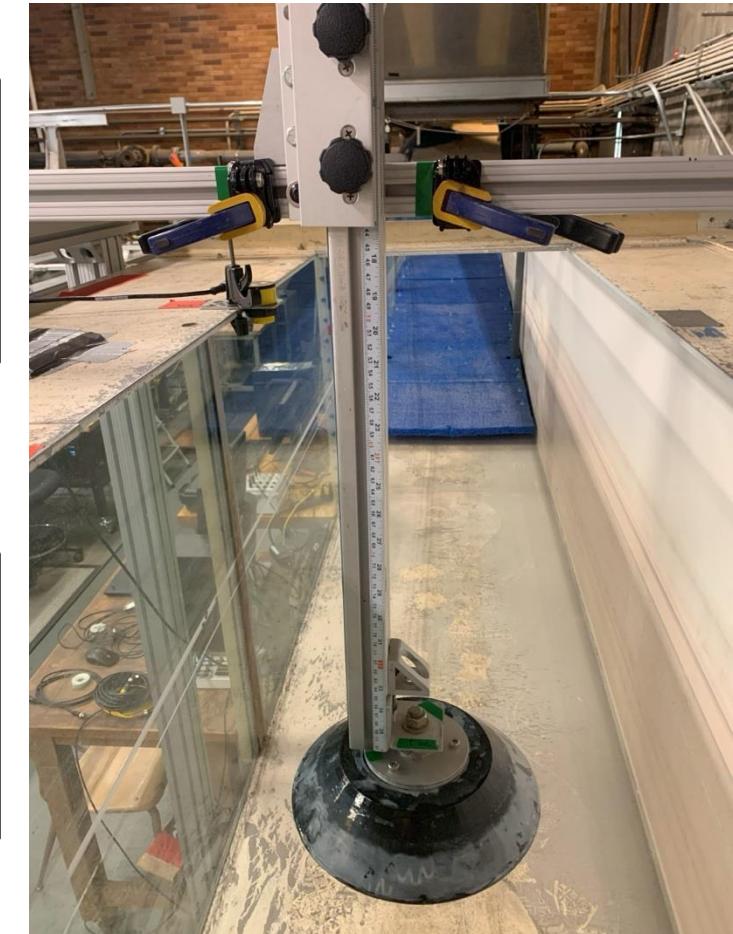
Experimental Methods



Experimental Methods



→
Wave Propagation



WEC Hydrodynamics

From BEM:

$$F_{excitation} = F_{reaction}$$

$$F_{excitation} = H_3(\omega)\eta$$

Wave amplitude

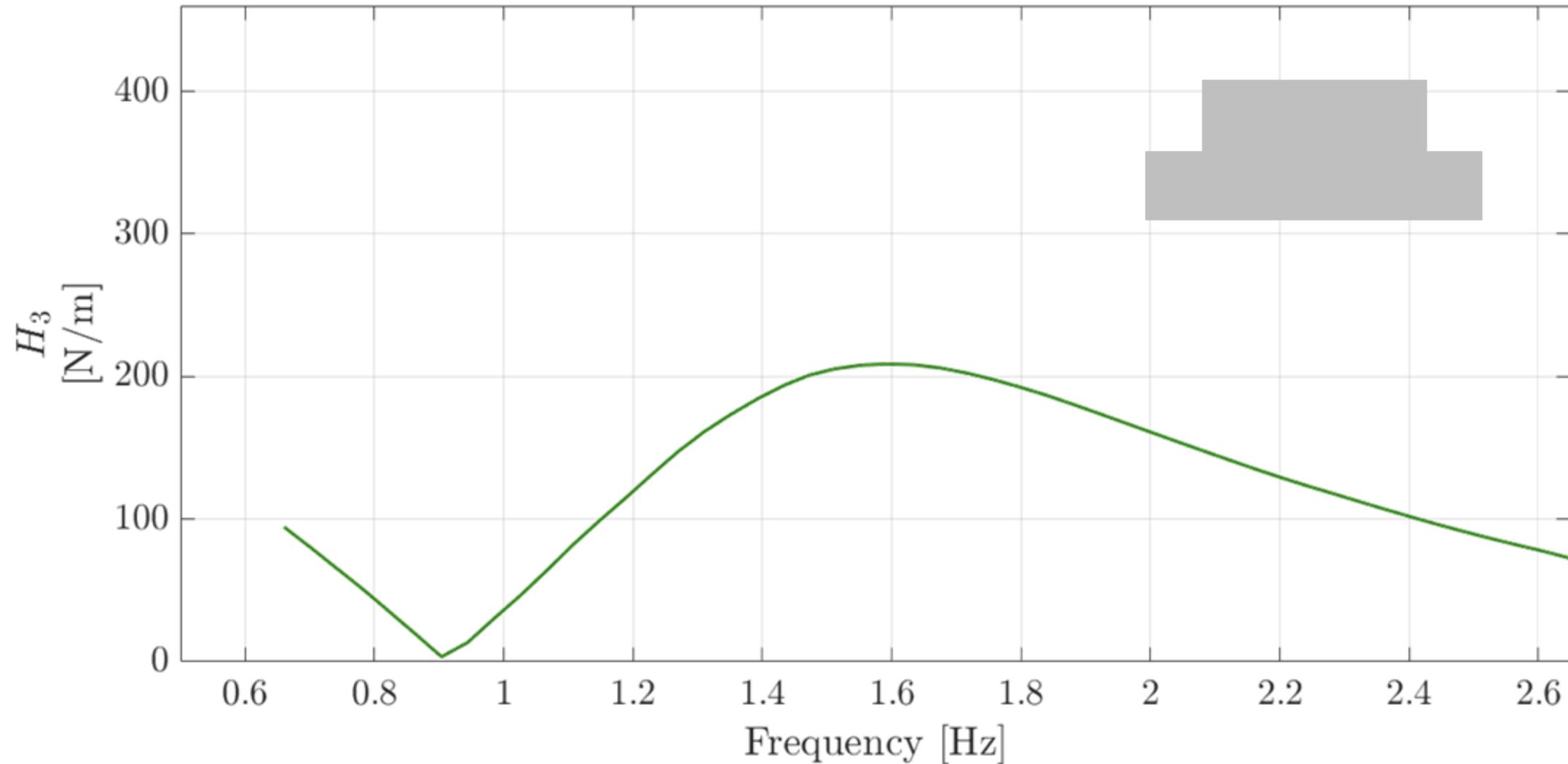
From Experiments:

$$H_3(\omega, \hat{\eta})\eta = F_R \quad \leftarrow \text{Measured heave force}$$

$$H_3(\omega, \hat{\eta}) = \frac{\widehat{F}_R}{\hat{\eta}} \quad \leftarrow \text{Amplitude of measured force}$$

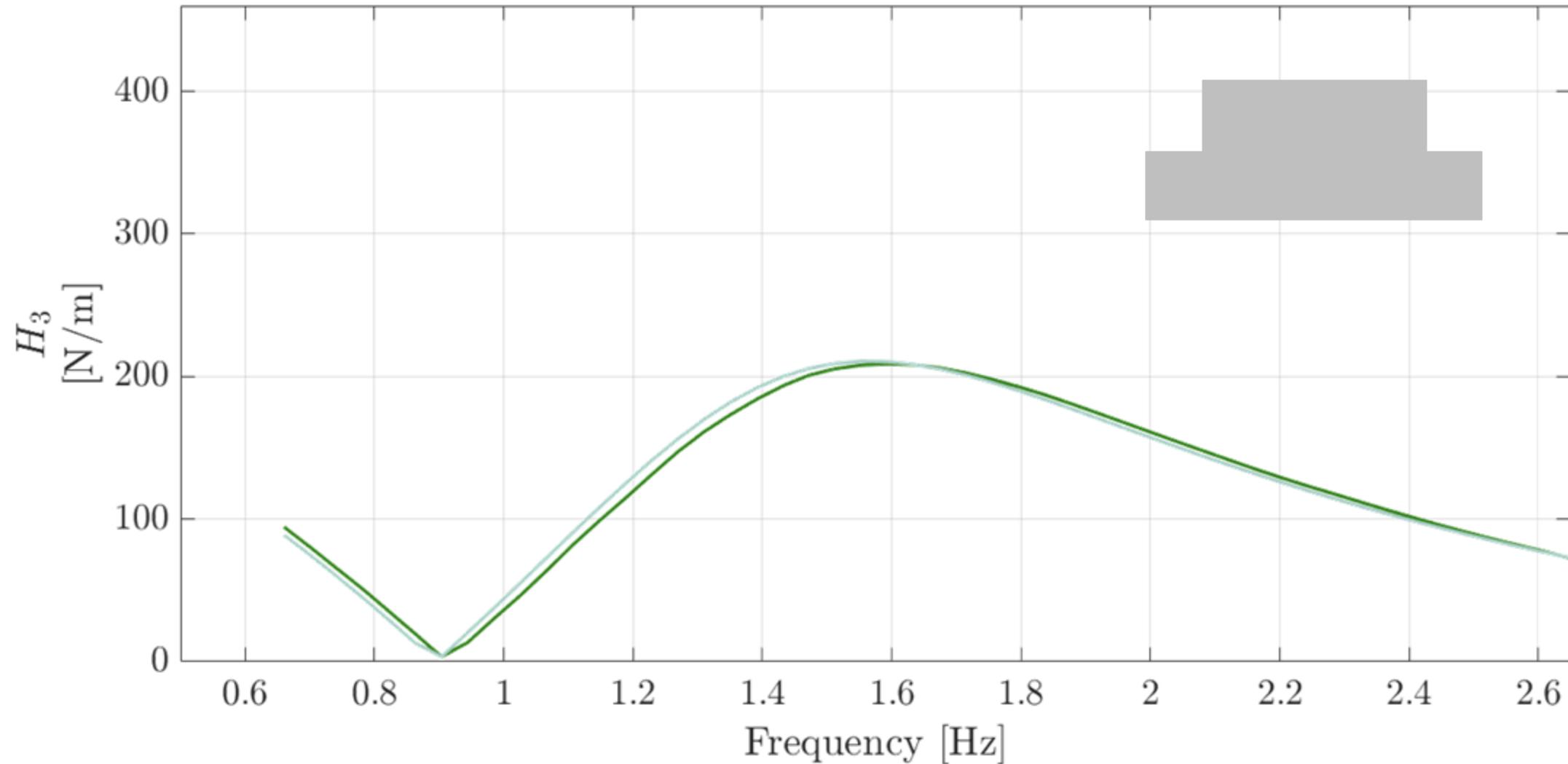
Wave Excitation Coefficients

— Capytaine — WAMIT - - WAMIT-Channel • $\hat{\eta} = 0.58 \text{ cm}$ ✕ $\hat{\eta} = 1.15 \text{ cm}$ □ $\hat{\eta} = 2.3 \text{ cm}$



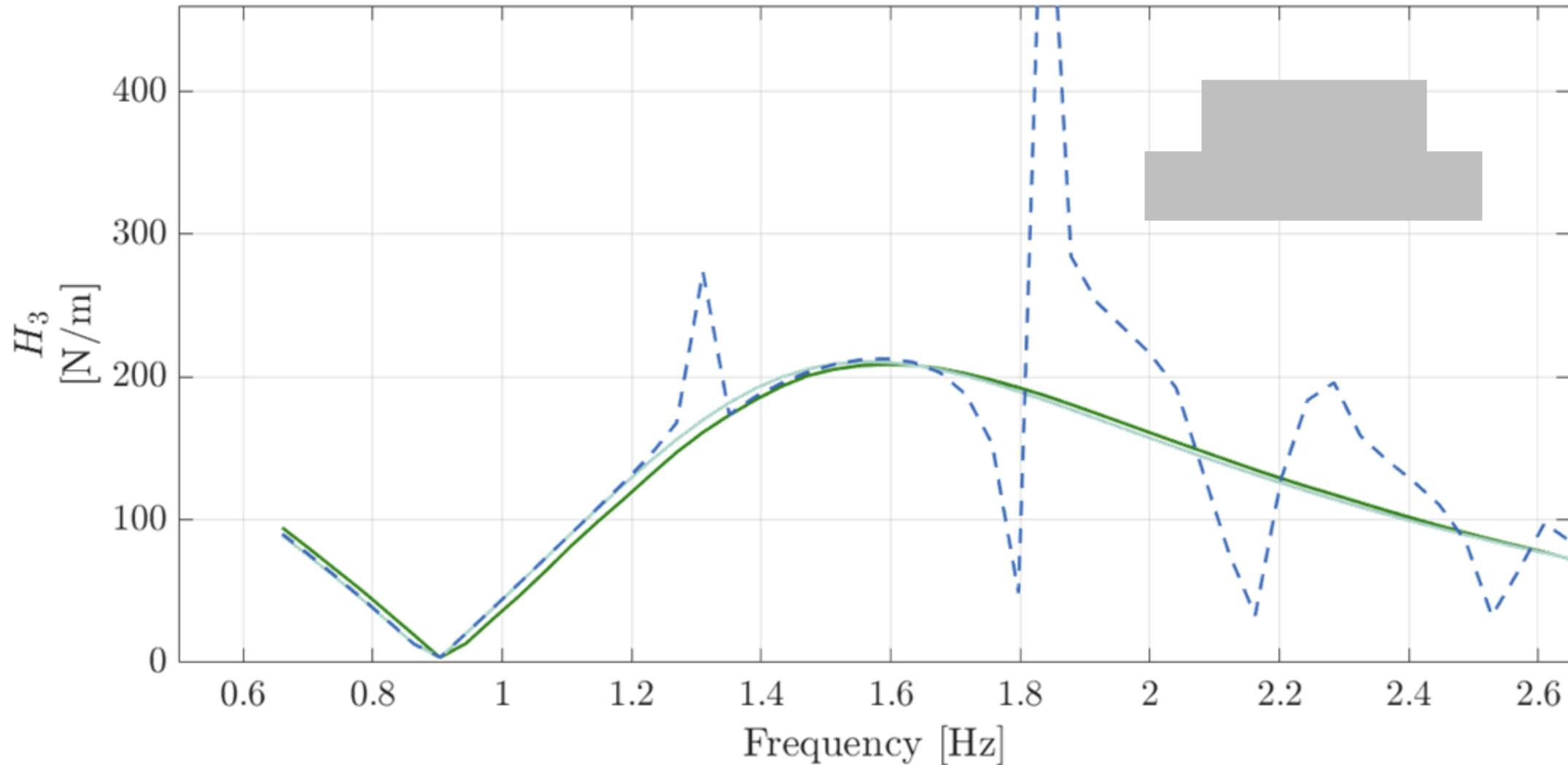
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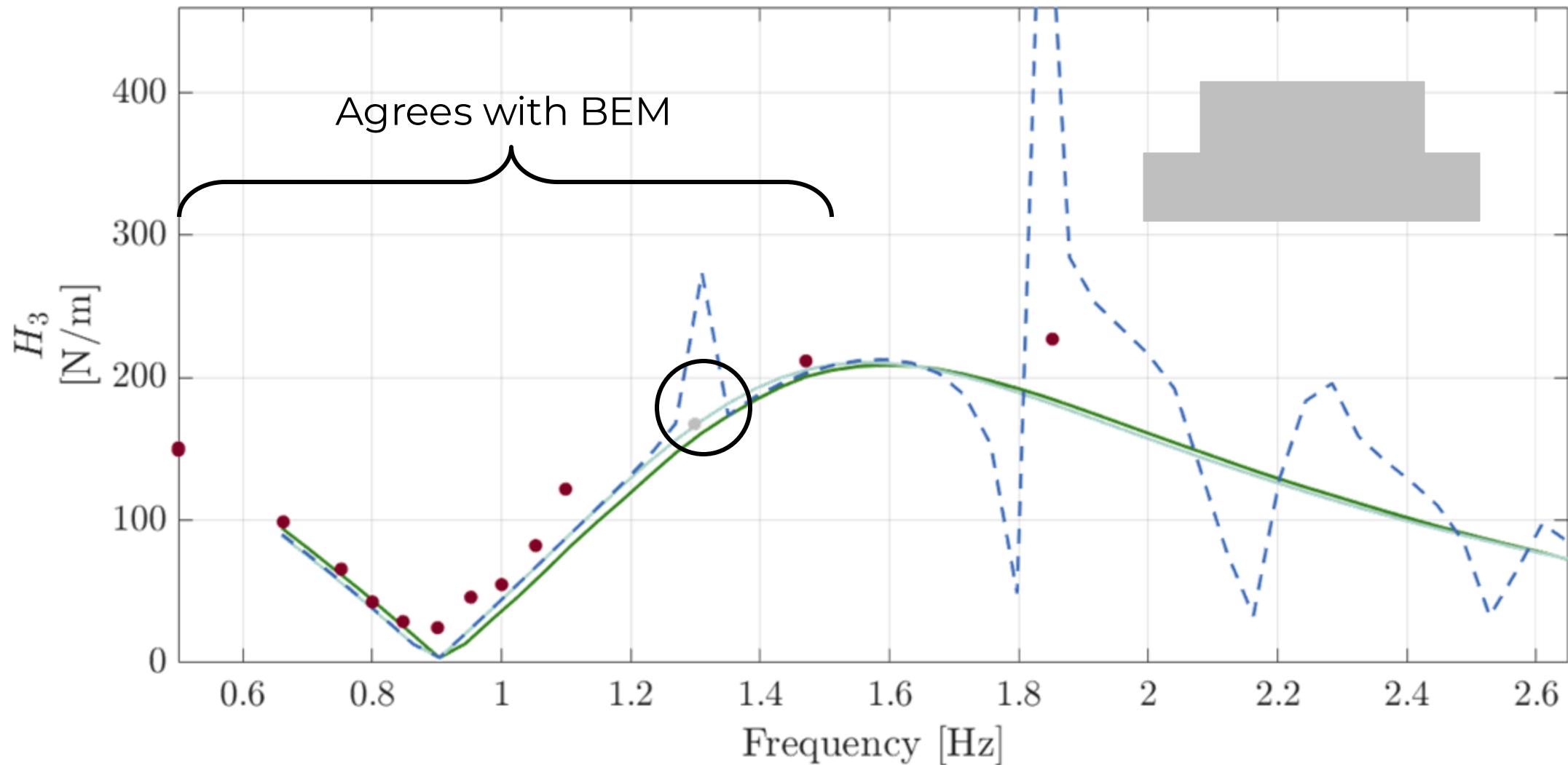
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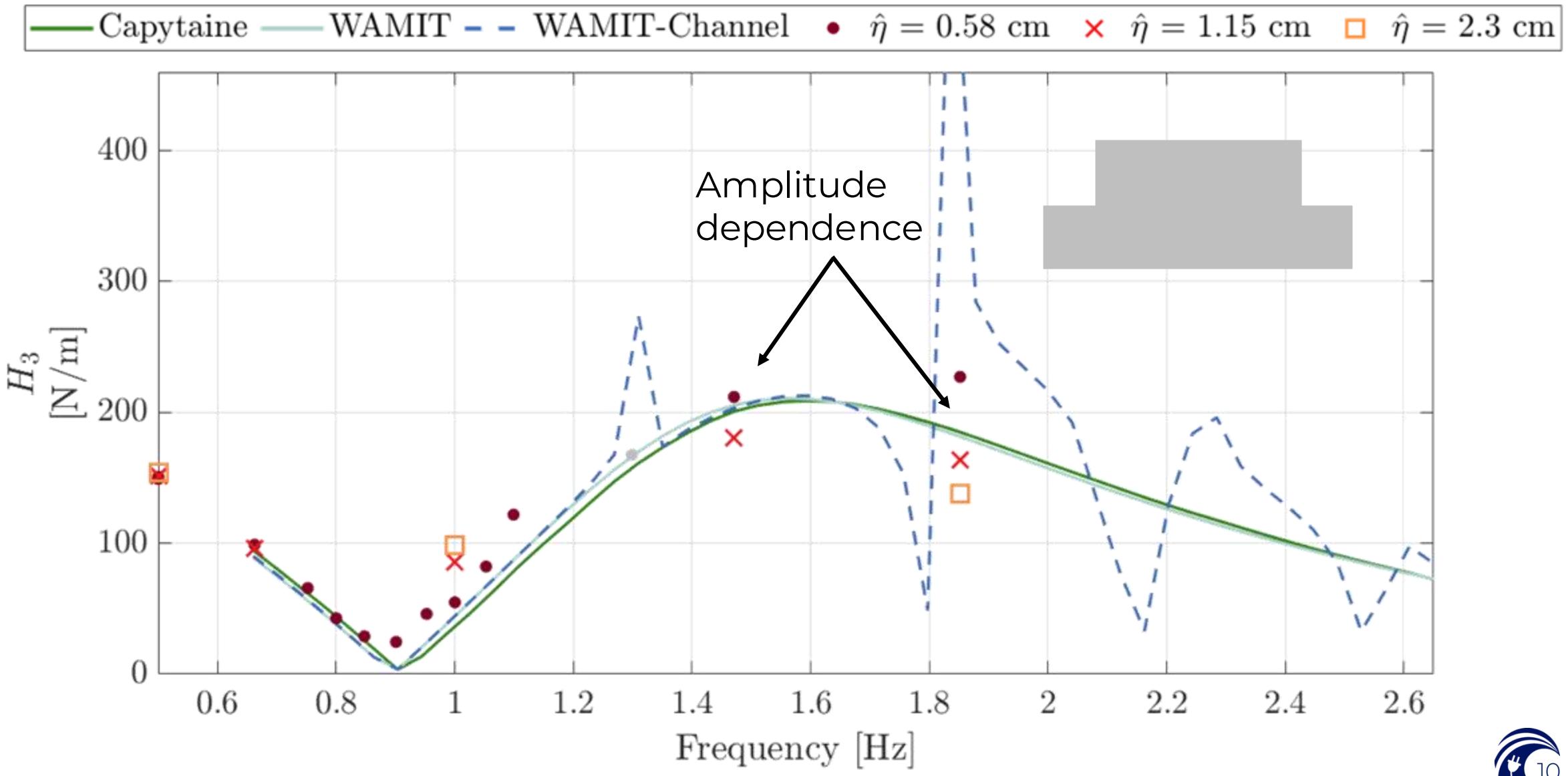


Wave Excitation Coefficients

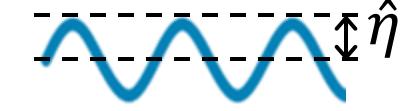
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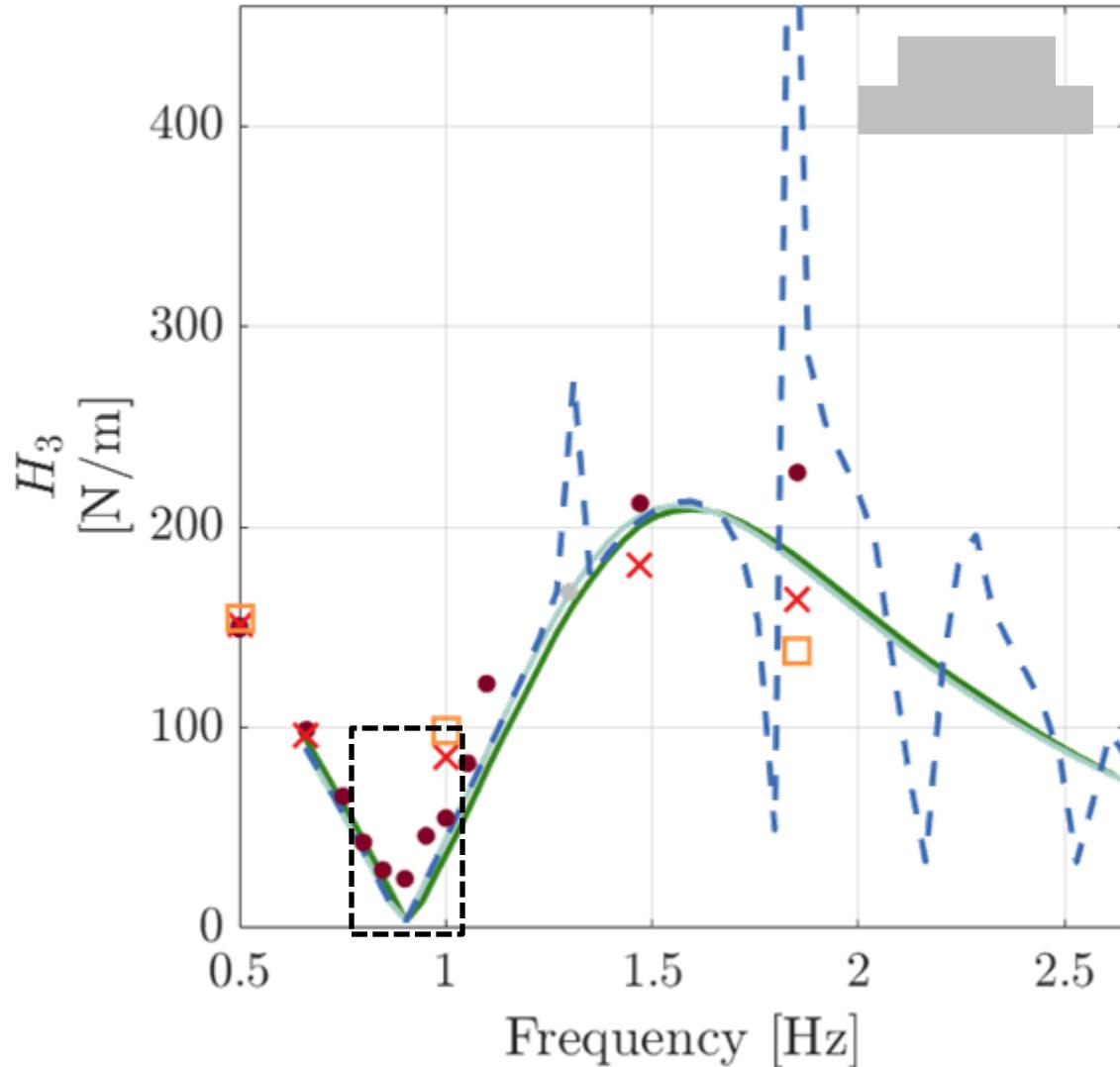
Wave Excitation Coefficients



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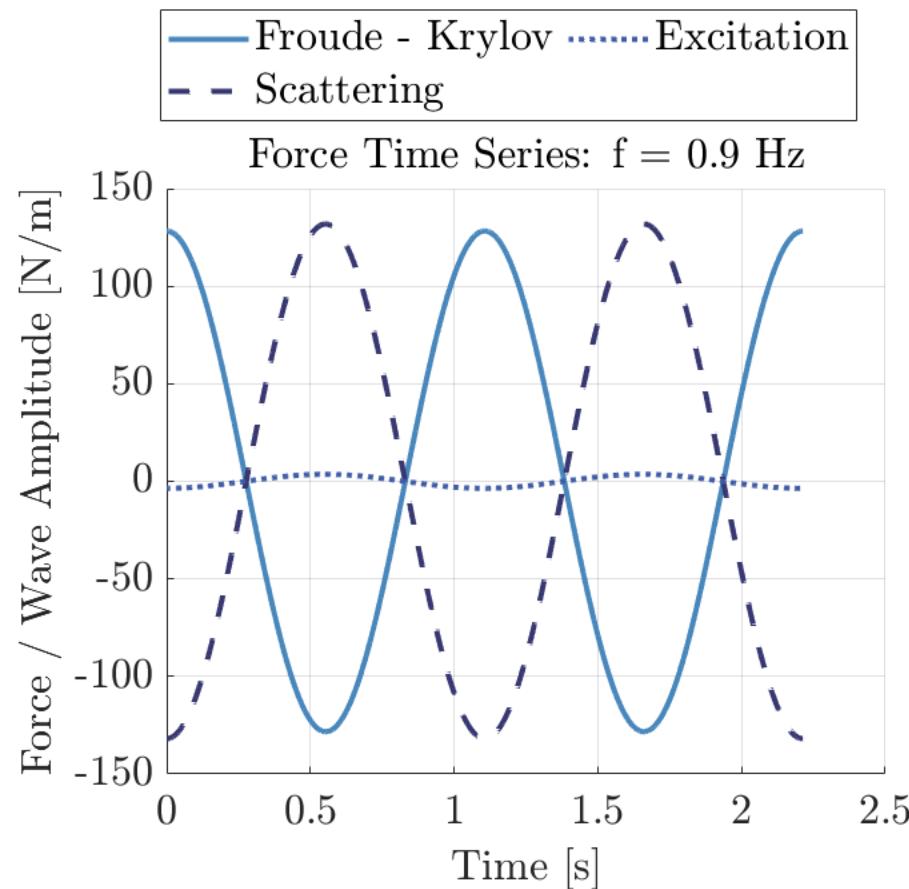
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Cancellation Frequency



$$H_3(\omega, \hat{\eta})\eta = F_{excitation}$$



Time Domain Reconstructions

$$H_3(\omega, \hat{\eta})\eta = F_{excitation} = H_3\hat{\eta}\cos(\omega t + \phi_{ex})$$

Measured force

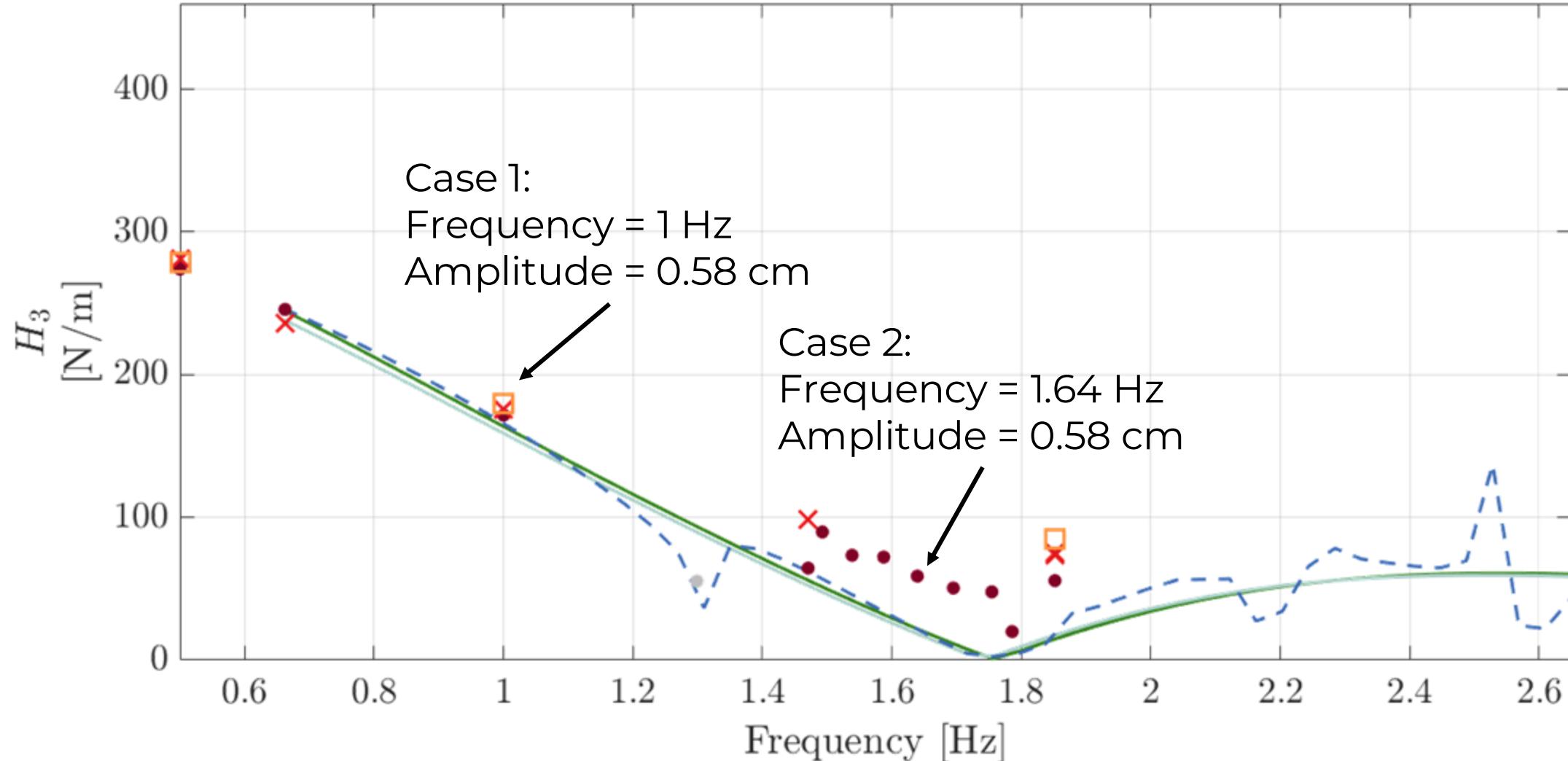
$$F_R$$

Compare to evaluate the accuracy of the linear assumption

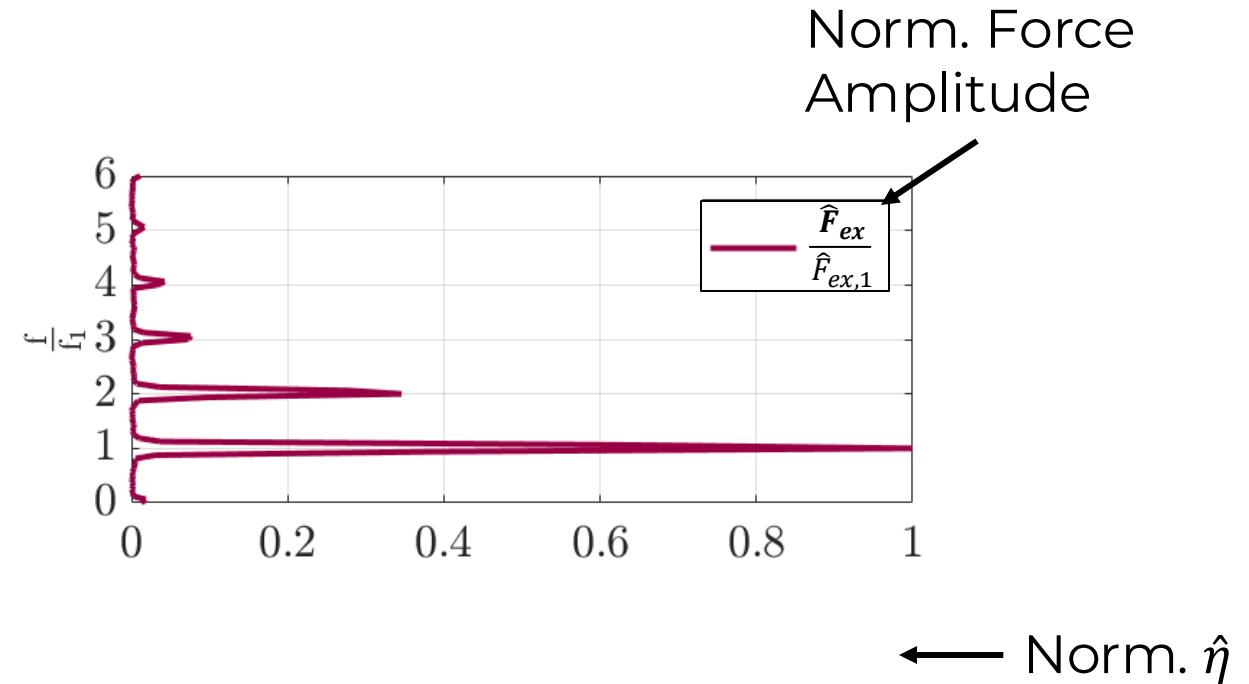
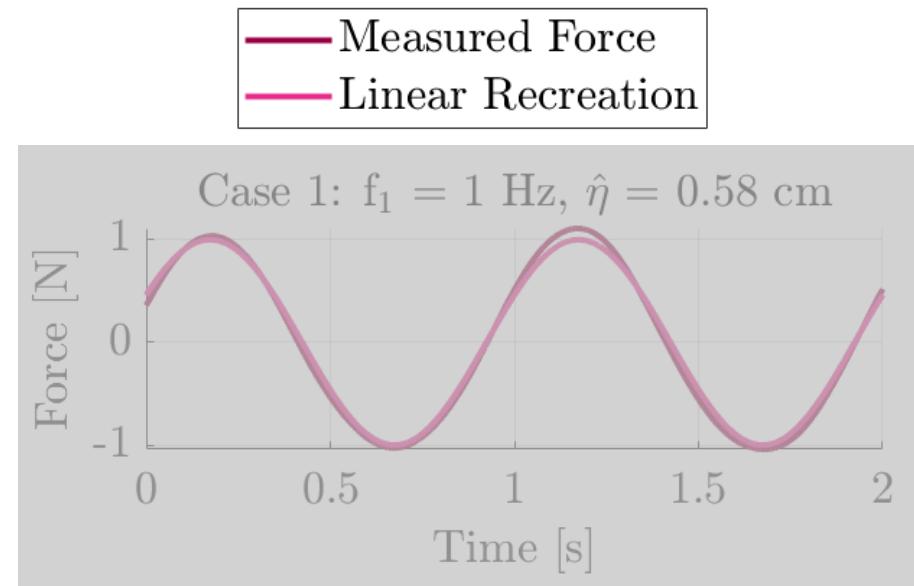
Wave Excitation Coefficient



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Time Domain Reconstructions



Conclusions / Next Steps

- WAMIT and Capytaine results agree for both floats
- Experimental H_3 agree with BEM at low frequencies, and disagree at high frequencies
- Destructive interference of the Froude-Krylov force and scattering force cause nulls in H_3
- The first harmonic wave excitation signal is not fully descriptive of the measured force signal
 - This could be due to experimental artifacts



Thank You

Acknowledgements:

- Gemma Calandra
 - model manufacturing
 - Additional wave excitation experiments



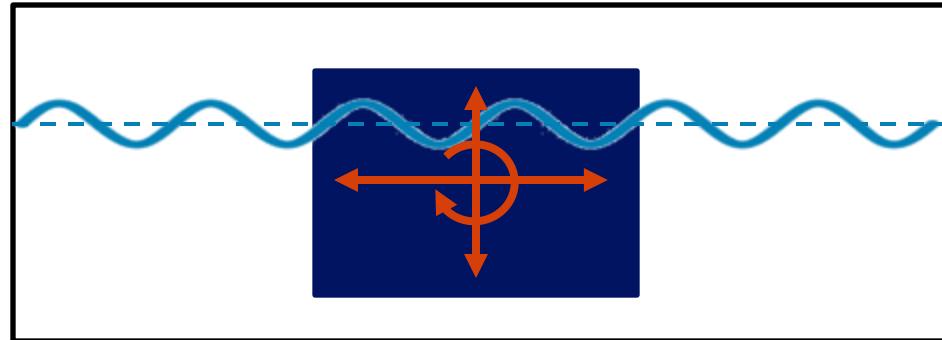
Questions:

smp52@uw.edu

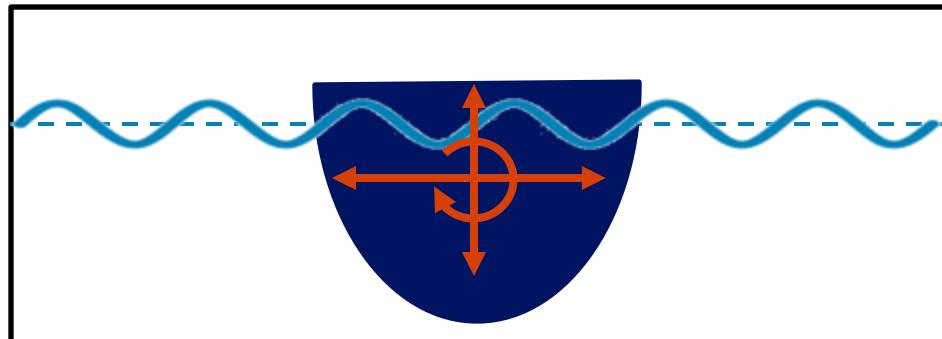


Appendix

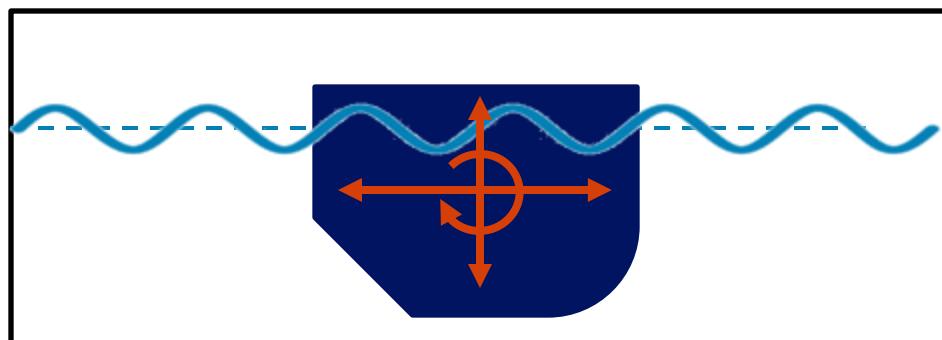
Point-Absorber Float Hydrodynamics



- WEC float geometry is an important design driver
 - requires accurate characterization of hydrodynamic response



- Float hydrodynamics are often characterized via experiments or boundary element method simulations (BEM)



Project Goals

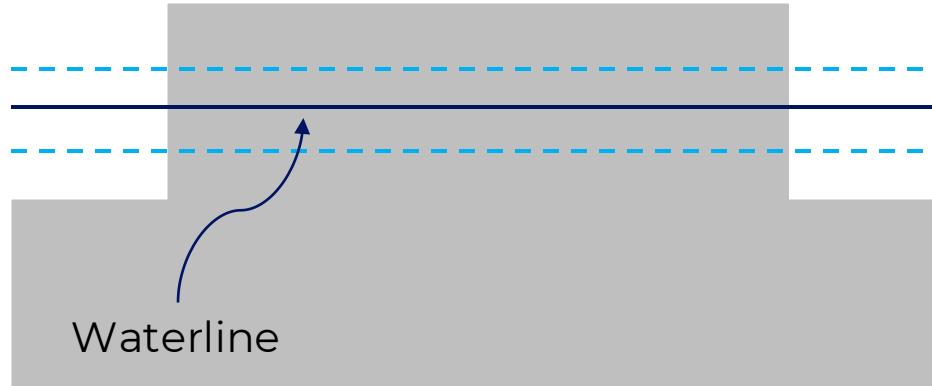
Compare hydrodynamic coefficients from experiments and Boundary-Element-Methods (BEM) across various float geometries?

This Presentation

1. Compare **wave excitation results** for four float geometries in heave
2. Identify the source of **cancellation frequency** behavior in the wave excitation force coefficient
3. Compare the measured force signals to **time domain recreations** using linear hydrodynamics assumptions

Geometries

Hat



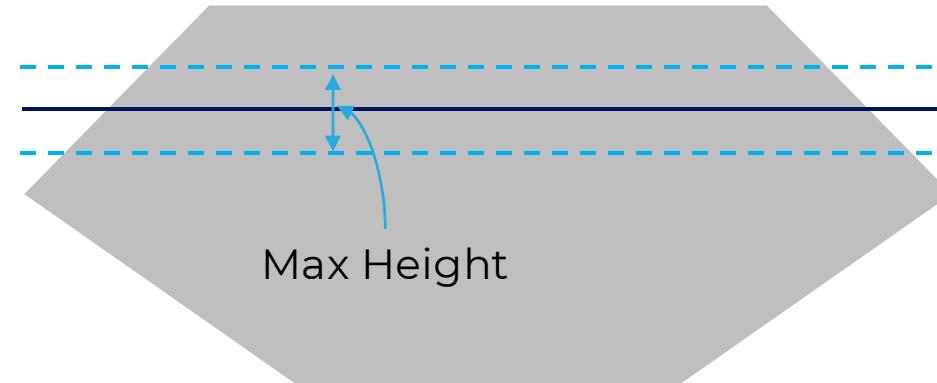
T – Shape



Ring



Diamond



WEC Hydrodynamics

$$(A_{33}(\omega) + M)\ddot{z} + B_{33}(\omega)\dot{z} + K_{33}z = H_3(\omega)\eta + F_a$$

PTO Force

Radiation Term

Heave excitation coefficient

Wave elevation

$$H_3(\omega, \hat{\eta})\eta = F_R \leftarrow \text{Measured heave force}$$

$$H_3(\omega, \hat{\eta}) = \frac{\widehat{F}_R}{\hat{\eta}} \leftarrow \begin{array}{l} \text{Amplitude of measured force} \\ \text{Wave Amplitude} \end{array}$$

Cancellation Frequency

$$H_3(\omega, \hat{\eta})\eta = F_{excitation} = F_{incident} + F_{scattering}$$

Froude – Krylov Force Scattering or Diffraction

$H_3 \hat{\eta} \cos(\omega t + \phi_{ex})$

Wave Amplitude

Wave frequency

From BEM