

*Molecular Simulation of a Hydrated Cation
Exchange Membrane System Used in Reverse
Electrodialysis*

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PRINCIPLE OF REVERSE ELECTRODIALYSIS

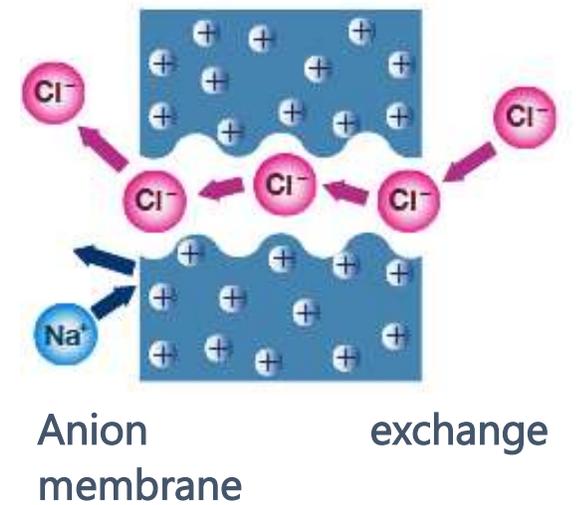
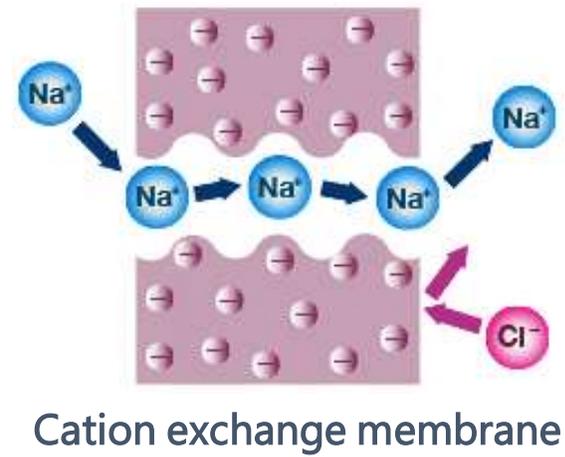
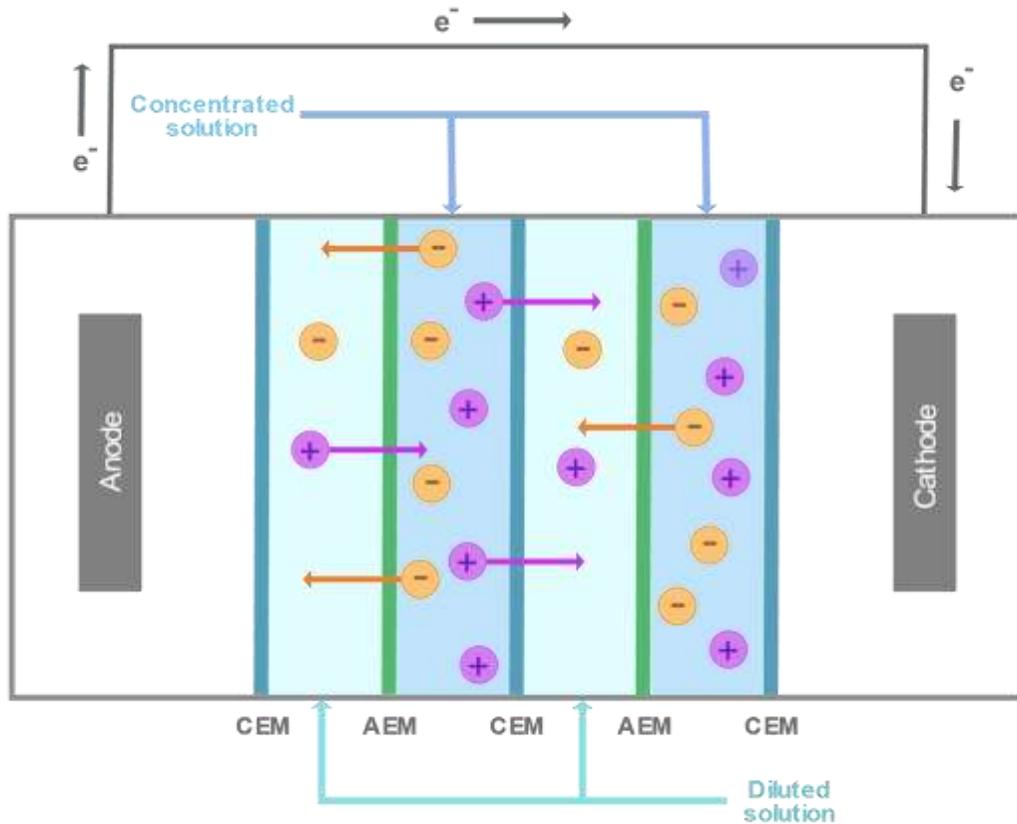


Fig. 1. Schematic representation of the reverse electrodialysis technology.

Effect of Multivalent Ions

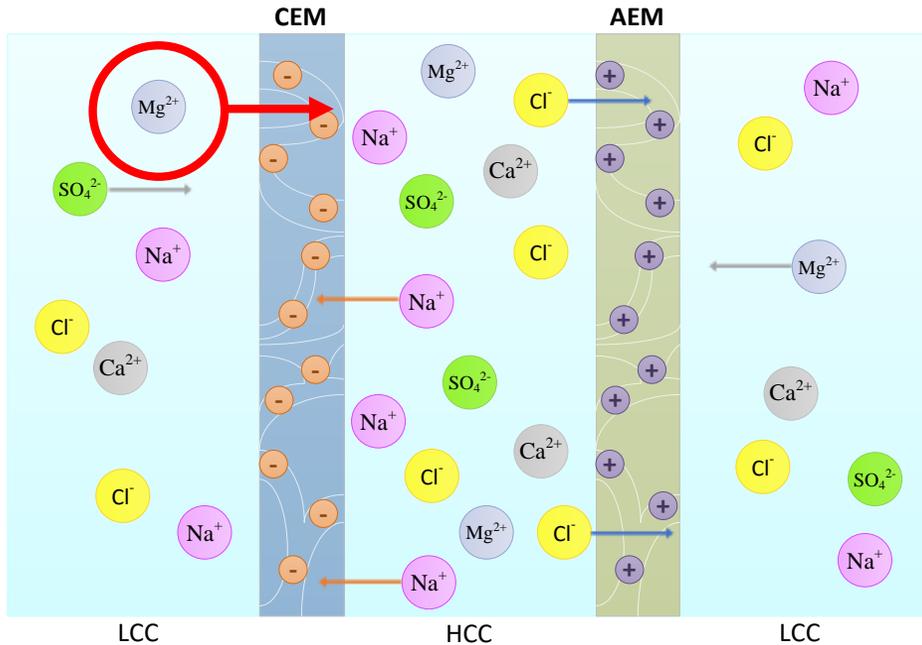
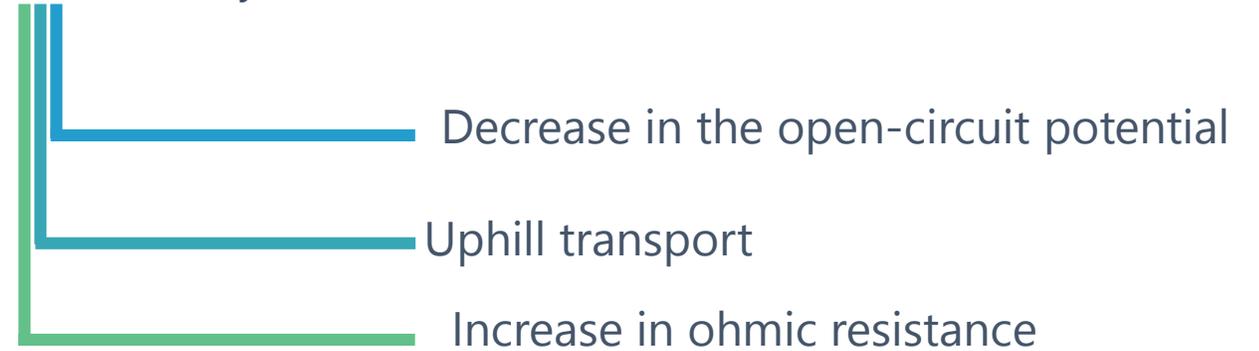


Fig. 2. RED system

- Power density is halved



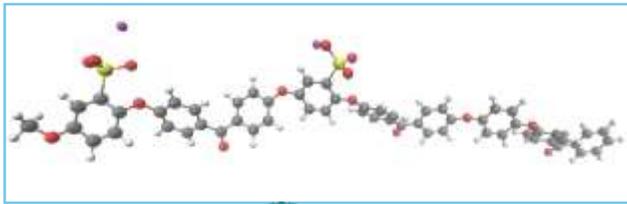
- Efforts to mitigate side effects consist mainly in the modification of ion exchange membranes.
- CEMs are more susceptible to the effect of multivalent ions.
- Lots of experimentation, lack of theoretical basis.

How does the presence of divalent ions impact the efficiency of ion exchange, and how does it affect the diffusion behavior and mobility of ions?

Computational Tools

Molecular simulations provide information on length scales ranging from atomic to nanoscopic, and on time scales from nano to milliseconds.

Density Functional Theory (DFT)



Molecular Dynamic (MD) simulations

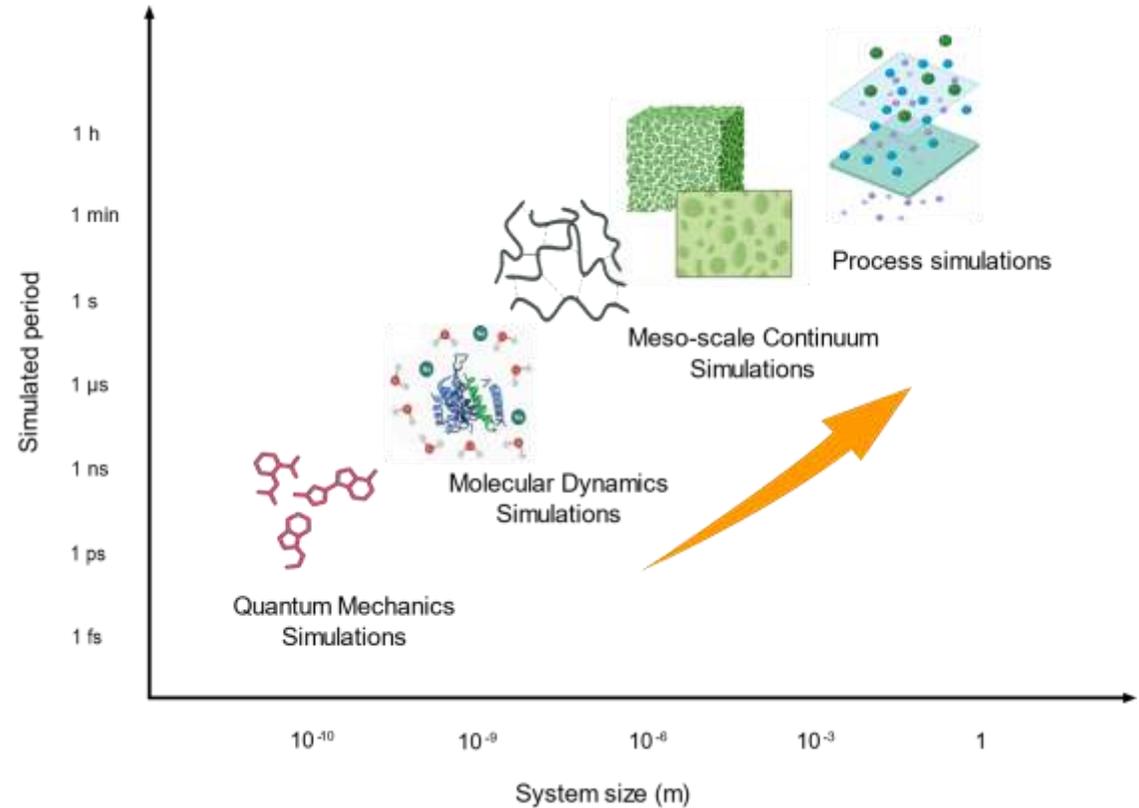
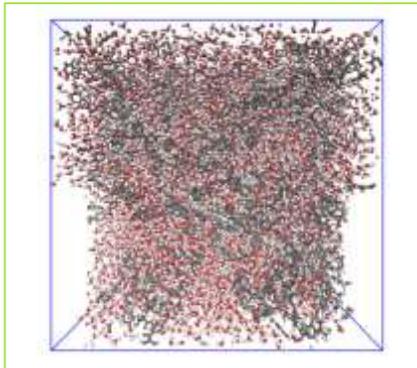
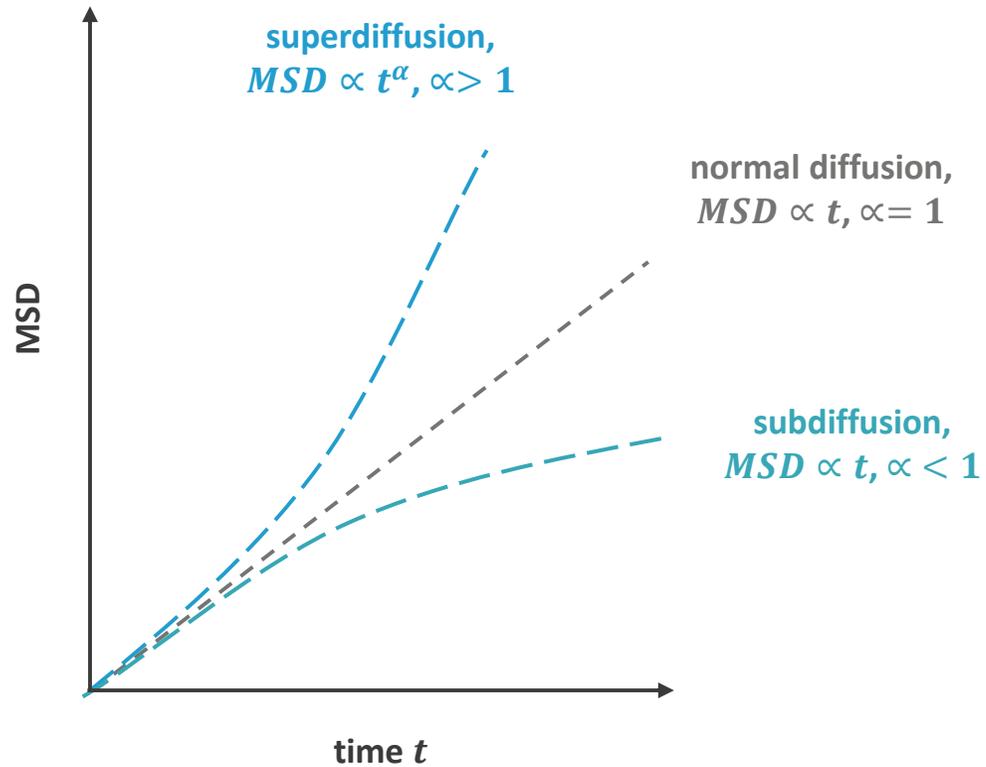


Fig. 3. Time scale vs system size of different simulation methods.

Self-diffusion Coefficient



From Mean Squared Displacement (MSD):

$$D = \frac{1}{6} \lim_{t \rightarrow \infty} \frac{d(MSD)}{dt}$$

For sufficiently long times:

- Linear trend for the MSD vs. time plot.
- Slope (α) of the $\log_{10}(MSD)$ vs. $\log_{10}(\text{time})$ plot should approach unity.

Fig. 5. Mean Squared Displacement (MSD) for different types of diffusion.

Values between 0.8 and 1 are satisfactory for considering the diffusion as normal.

Results: Self-diffusion Coefficients

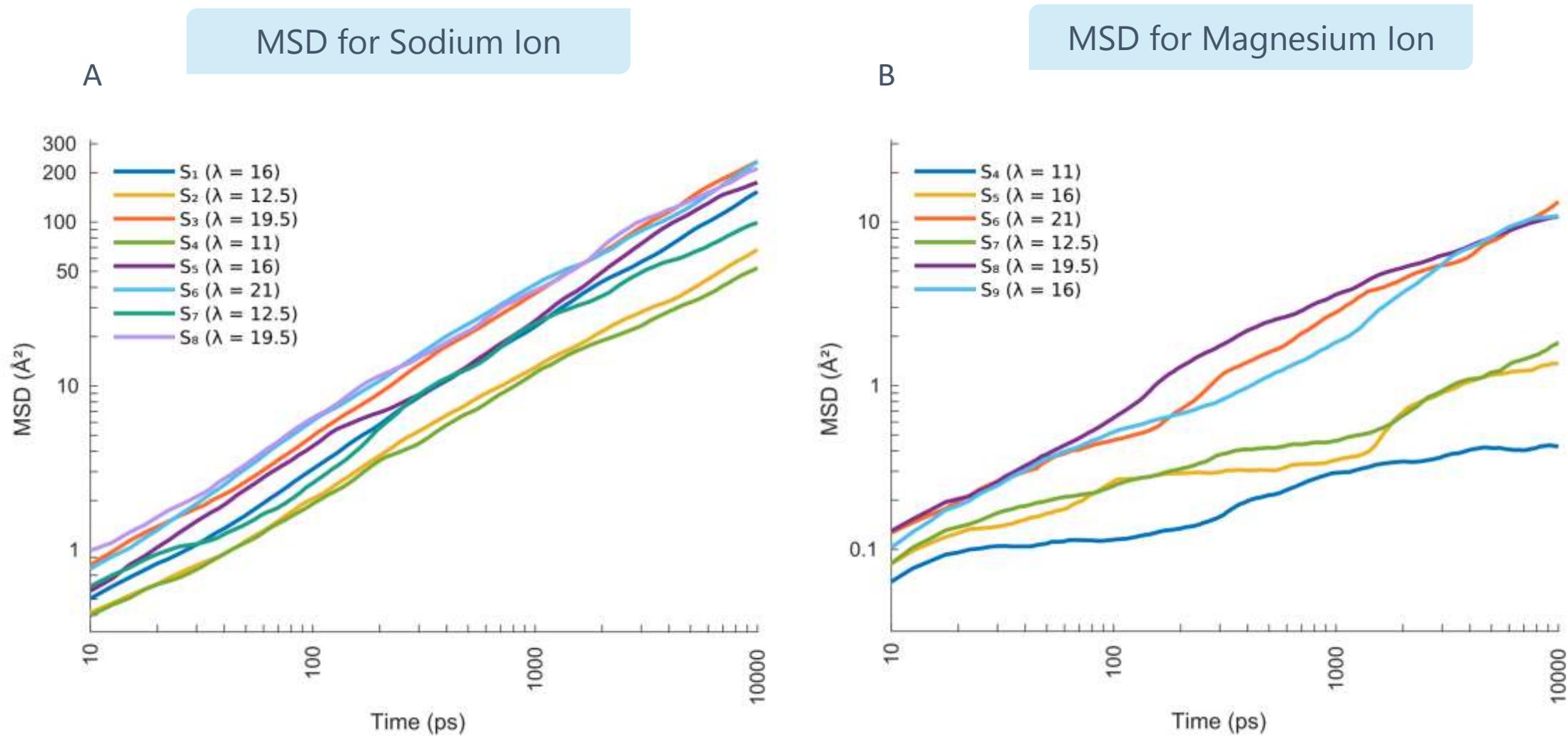
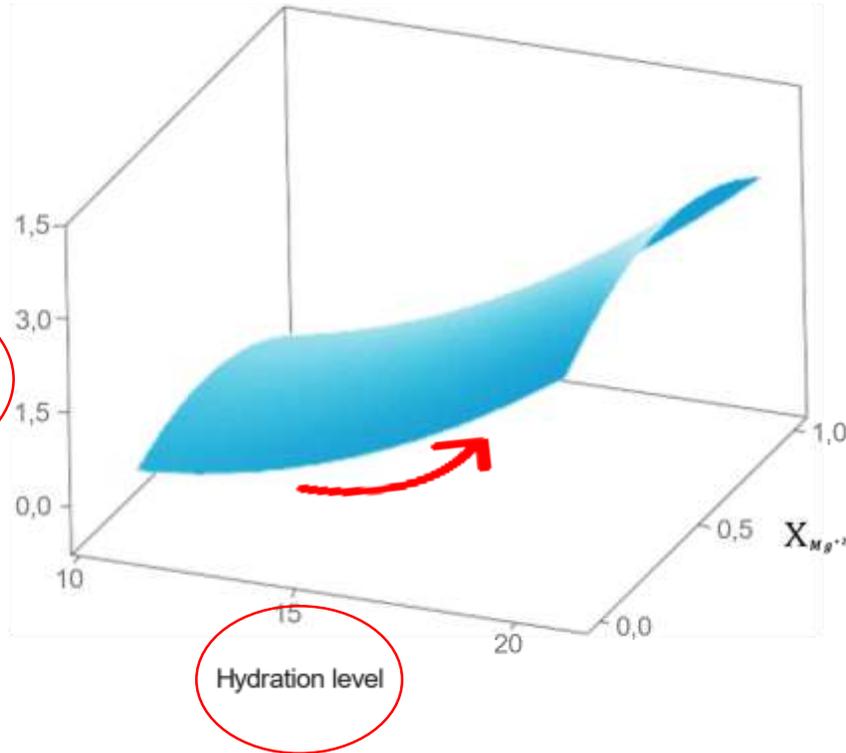


Fig. 6. The Mean Squared Displacement is displayed on the left side (A) for sodium ions and on the right side (B) for magnesium ions.

Results: Self-diffusion Coefficients



- Increase in the coordination number of ions or fixed charged groups is not observed as the degree of hydration increases.
- In cases of lower hydration levels, there is a more pronounced tendency towards subdiffusion.

Results: Transport of ions in a CEM

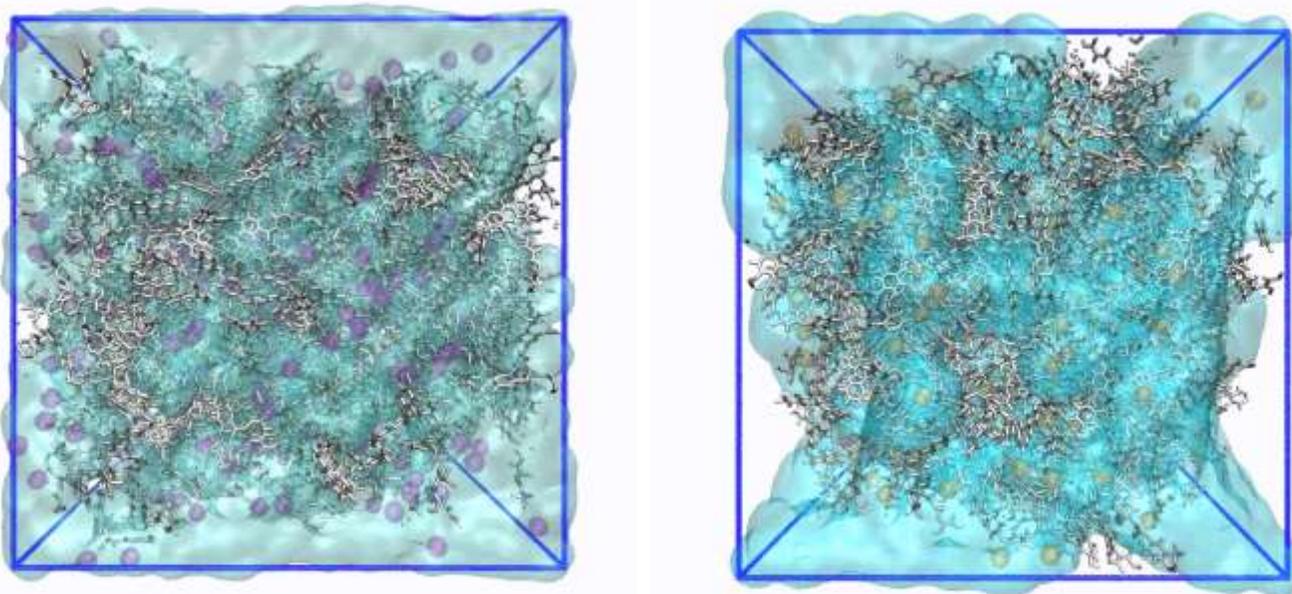


Fig. 8. MD simulations: (A) Hydrated sPEEK polymer and Na^+ ions. (B) Hydrated sPEEK polymer and Mg^{2+} ions.

- In most simulations, Mg^{2+} follows a sub-diffusive behavior, characterized by α values below 0.5.

$$r^2(t) = \text{MSD} \sim 6D_\alpha t^\alpha$$

- The self-diffusion coefficient for magnesium is ten times lower than the self-diffusion coefficient for sodium.

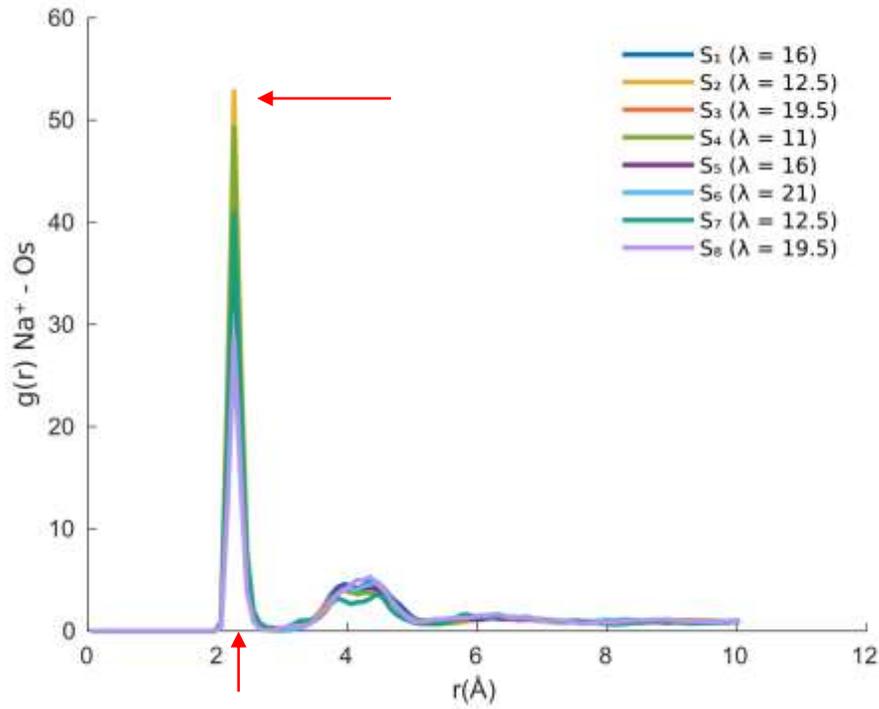
Membrane

$$\frac{D_{\text{Mg}^{2+}}}{D_{\text{Na}^+}} = 0.122$$

Solution

$$\frac{D_{\text{Mg}^{2+}}}{D_{\text{Na}^+}} = 0.502$$

Sodium – sulfonate group



Magnesium – sulfonate group

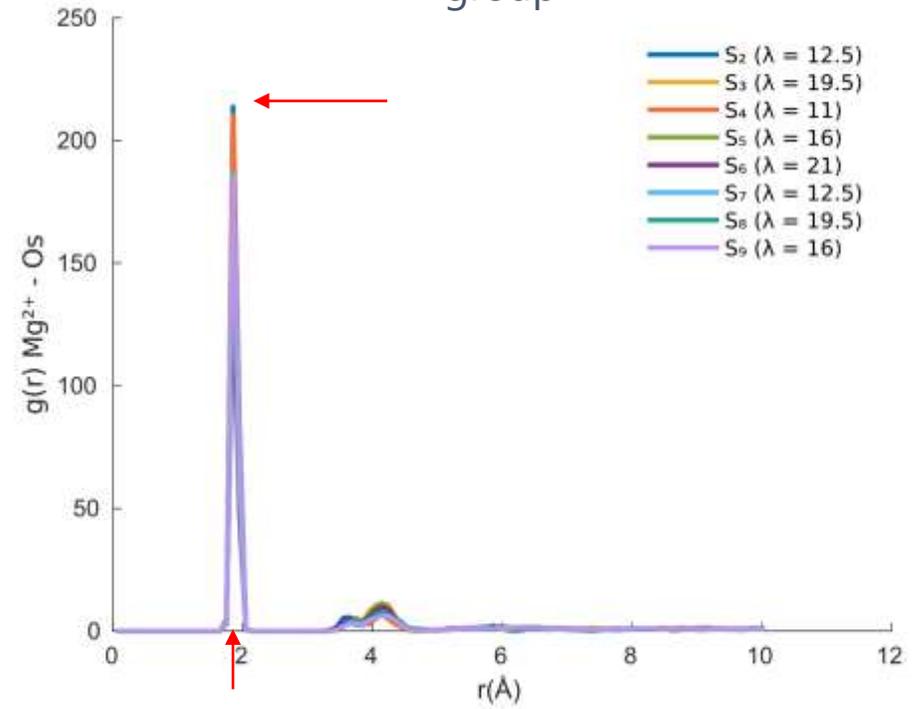
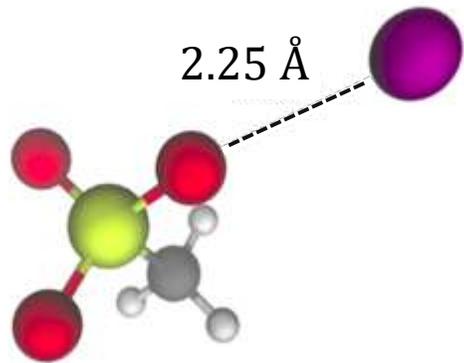
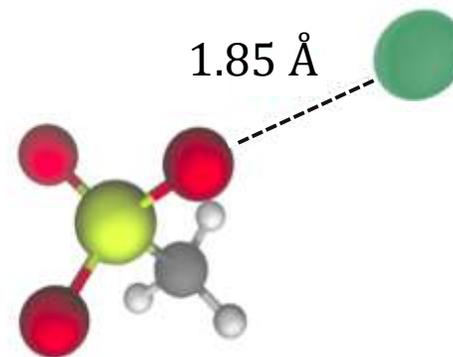


Fig. 9. Radial Distribution Function (RDF): A) Na⁺ - Os . (B) Mg²⁺ - Os.



$$E_{elec} = 21718 \frac{kcal}{mol}$$



$$E_{elec} = 32577 \frac{kcal}{mol}$$

- A stronger interaction is established between magnesium and the functional group.

Results: Anomalous Diffusion Coefficient

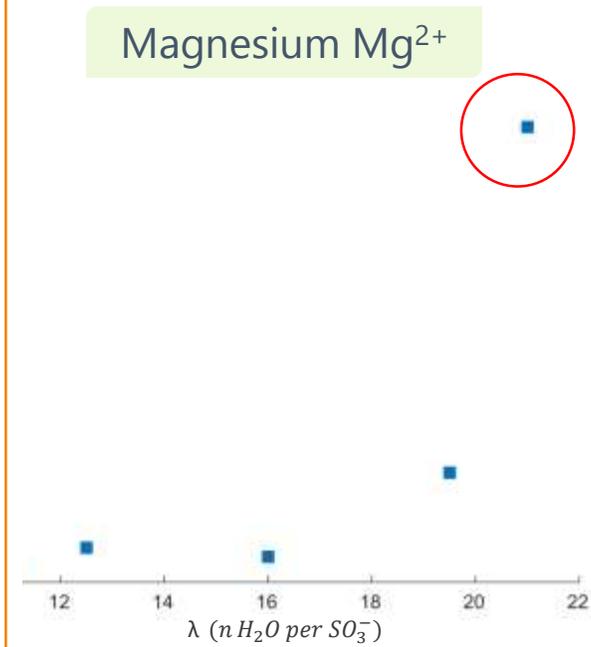
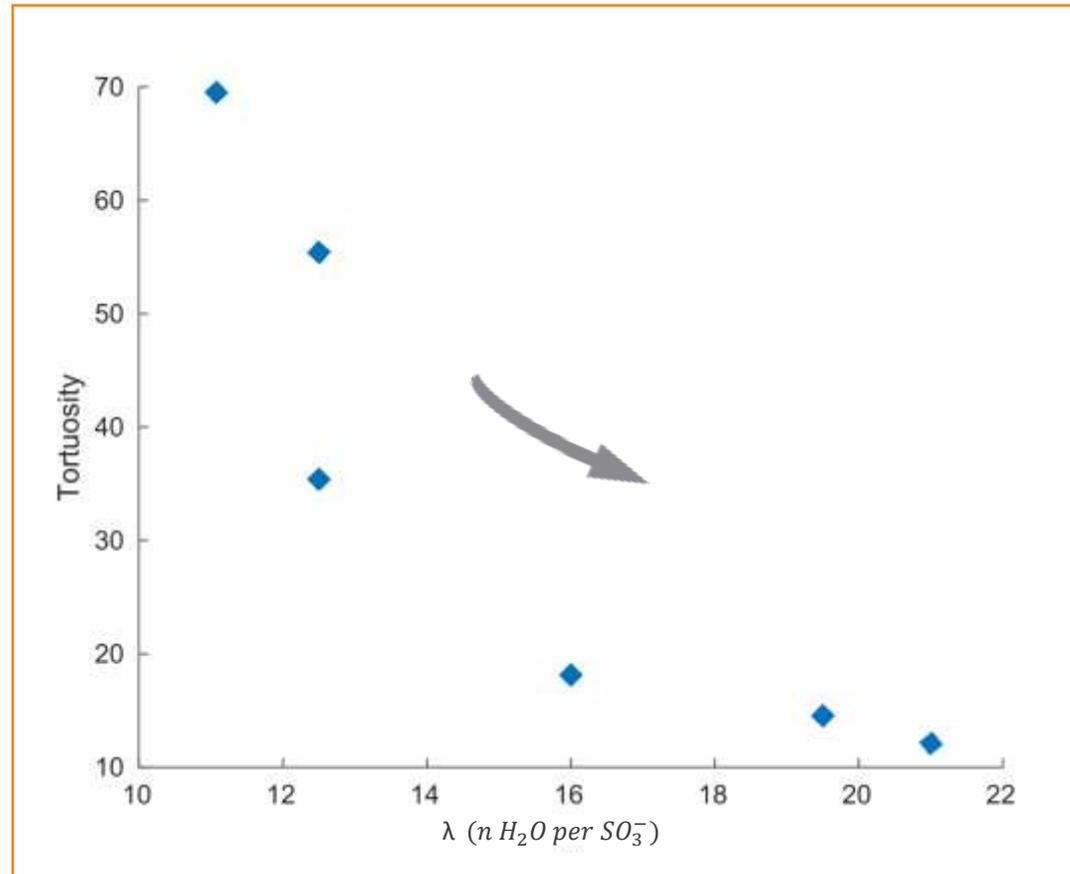
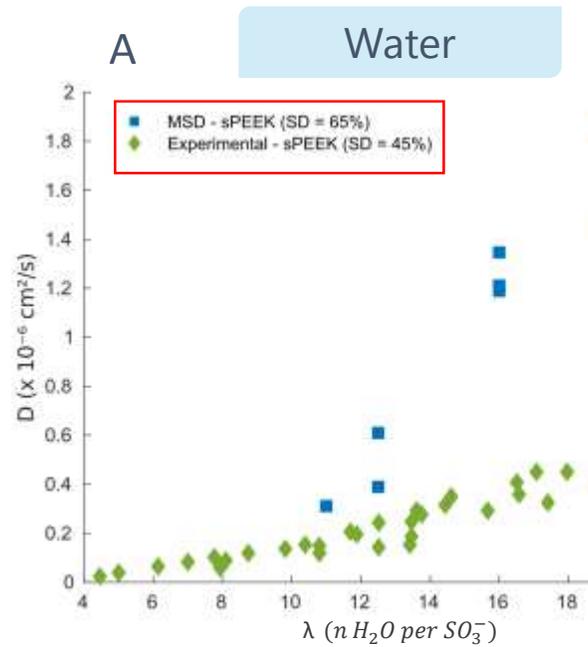


Fig. 10. (A) Water anomalous diffusion coefficient obtained from NMR measurements (Woudstra, J). (B) Tortuosity vs hydration number. (C) Mg^{2+} anomalous diffusion coefficient obtained from NMR measurements.

(C) Mg^{2+} anomalous diffusion coefficient obtained from NMR measurements.

Conclusions

- Magnesium ion has a lower mobility than sodium ion. A lower mobility leads to higher solution resistance, impacting the overall electrical conductivity of the system.
- The synthesis of ion exchange membranes with a more interconnected water network favors ion transport. Macroscopic properties such pore sizes (Pore-Limiting Diameter) and tortuosity can be tuned for the design of selective ion exchange membranes.
- Computational modeling and simulation techniques play a crucial role in understanding the transport dynamics of multivalent ions in RED systems.

Future Work

- Study the effect of coions: Manning's theory applied to systems with multiple ions to study the effect of ion condensation on the polymer.
- Simulation of ion transport in the presence of an electric field.
- Perform non-equilibrium molecular dynamics simulations.

Thank you

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